

Test generation using verification

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Adapted from

B. Jeannet, T. Jéron, V. Rusu, E. Zinovieva,
Symbolic Test Selection based on Approximate Analysis,
in TACAS'05, LNCS 3440, Edinburgh (Scotland), April 2005.

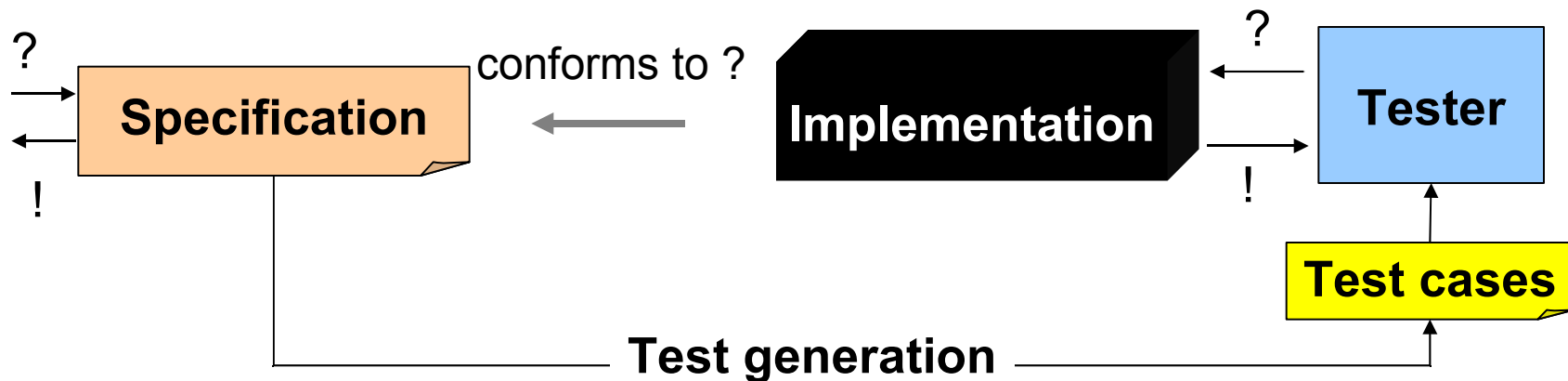
Vlad Rusu, Hervé Marchand, Thierry Jéron,
**Automatic Verification and Conformance Testing for Validating Safety Properties
of Reactive Systems,**
in Formal Methods 2005 (FM05), July 2005.

Conformance Testing of reactive systems

Problem:

check if a **black-box implementation** of a reactive system conforms to a given **specification** by experimenting with **test cases**

- the source code of the implementation is unknown (or not used)
- only the interface is known
- and can be controlled/observed by the environment



Outline

- The *ioSTS* model
- Conformance Testing Theory with *ioco*
- Test selection using approximate analysis
- Conclusion

1. The *ioSTS* model

$$\mathcal{S} = (V_S, \Theta_S, \Sigma, T_S)$$

with

- V_S : variables \ni loc
- Θ_S : initial condition

with unique solution

- $\Sigma = \Sigma_l \cup \Sigma_r \cup \Sigma_\tau$:

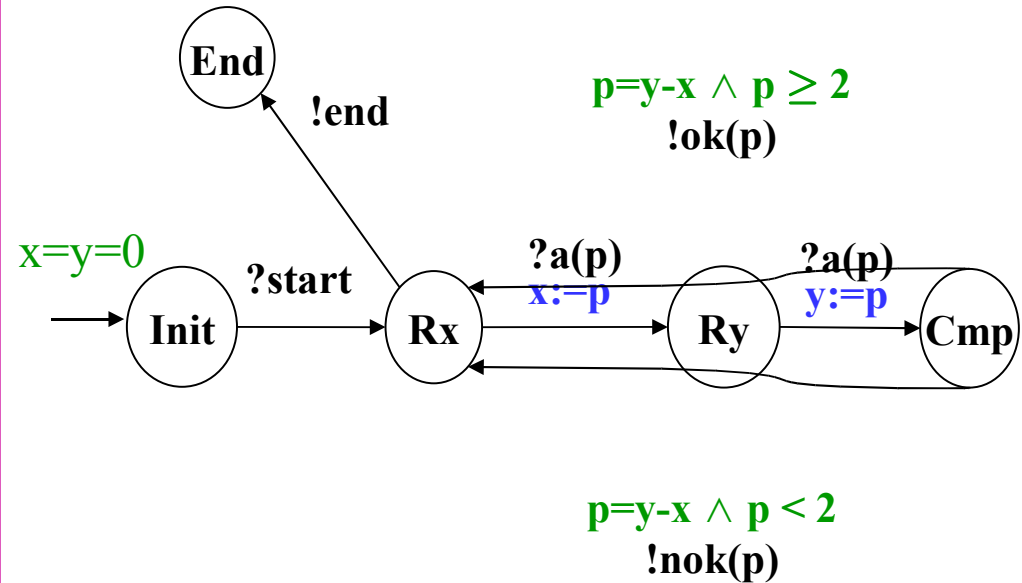
alphabet of actions

with comm. parameters P

- T_S : transition relation

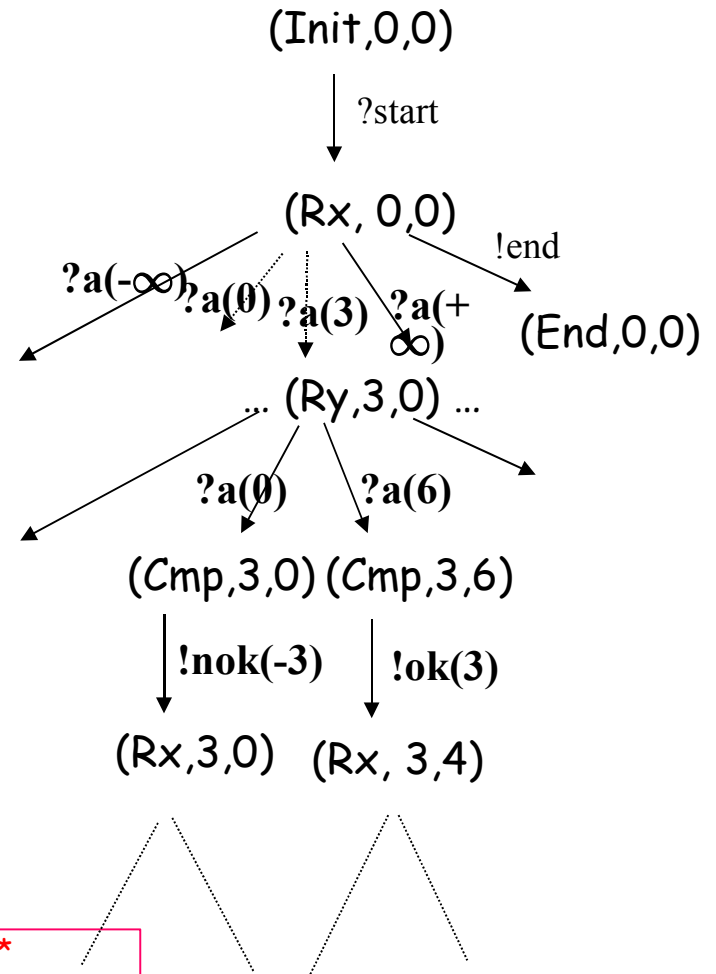
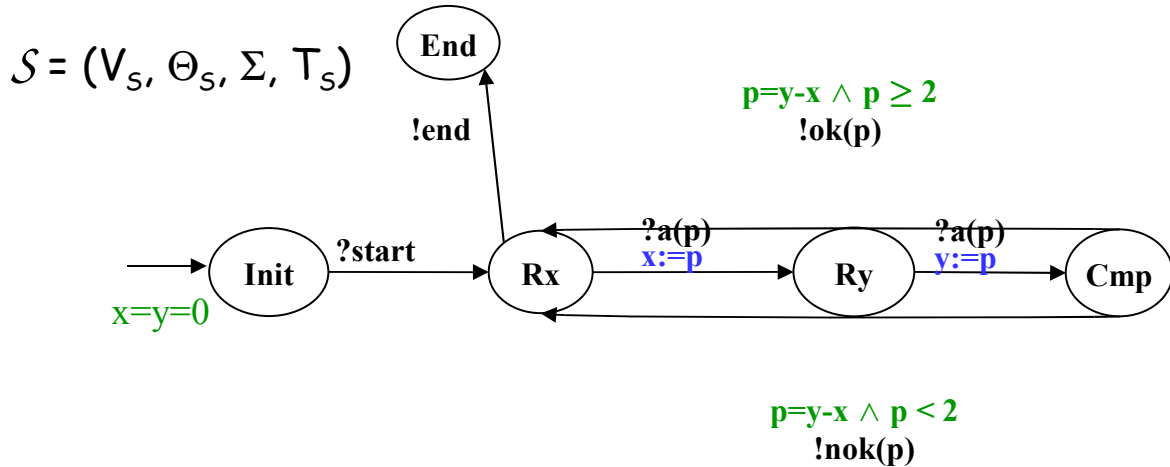
$[a(p) : G(v_S, p); v_S := A(v_S, p)]$

action guard assignment



Hyp: satisfiability of guards is decidable.

ioLTS semantics of ioSTS



$[[\mathcal{S}]] = S = (Q, Q_0, \Lambda, \rightarrow)$ with

- $Q = \prod_{v \in V_S} \text{Dom}(v)$ i.e. $q = \langle v_0, \dots, v_n \rangle$
- $Q_0 = \Theta_S = \{ \langle v_0, \dots, v_n \rangle \}$
- $\Lambda = \{ \langle a, \pi \rangle \mid a \in \Sigma \wedge \pi \in \text{Dom}(\text{sig}(a)) \}$
- $[a, p, G, A] \in T, q \in Q, \exists \pi \in \text{Dom}(\text{sig}(a)), G(q, \pi)$
 $q - a(\pi) \rightarrow q' = A(q, \pi)$

$\text{Runs}(S): q_0 \rightarrow^{a_1(\pi_1)} q_1 \rightarrow^{a_2(\pi_2)} q_2 \dots \in Q_0. (\Lambda.Q)^*$

$\text{Tr}(S) : \text{proj}_{\Lambda_{\text{vis}}}(\text{runs}(S))$

Simplifying assumptions on $ioSTS$ (for this talk)

1. $ioSTS$ are supposed to be deterministic

Determinisation of $ioSTS$ into $ioSTS$ is **not always possible**

⇒ restrictions needed e.g.

- No internal loop
- Finite lookahead

2. Quiescence is not treated here

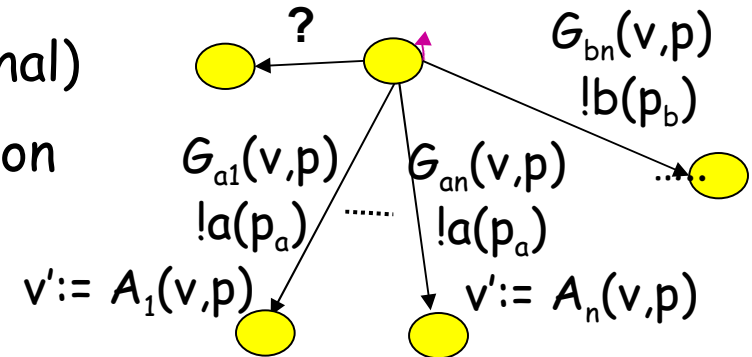
$\Delta(s)$: explicit quiescence by adding loops with $!\delta$
in all quiescent states (no fireable output/internal)

augment guard model with universal quantification

not a real problem

$$S\text{Tr}(S) = \text{Tr}(\Delta(S))$$

$$\mathbf{AE}_{a \in \Sigma_i \cup \Sigma_\tau} \mathbf{AE}_{t=[a,p,G,A]} \forall p, \neg G(v,p) \quad !\delta$$



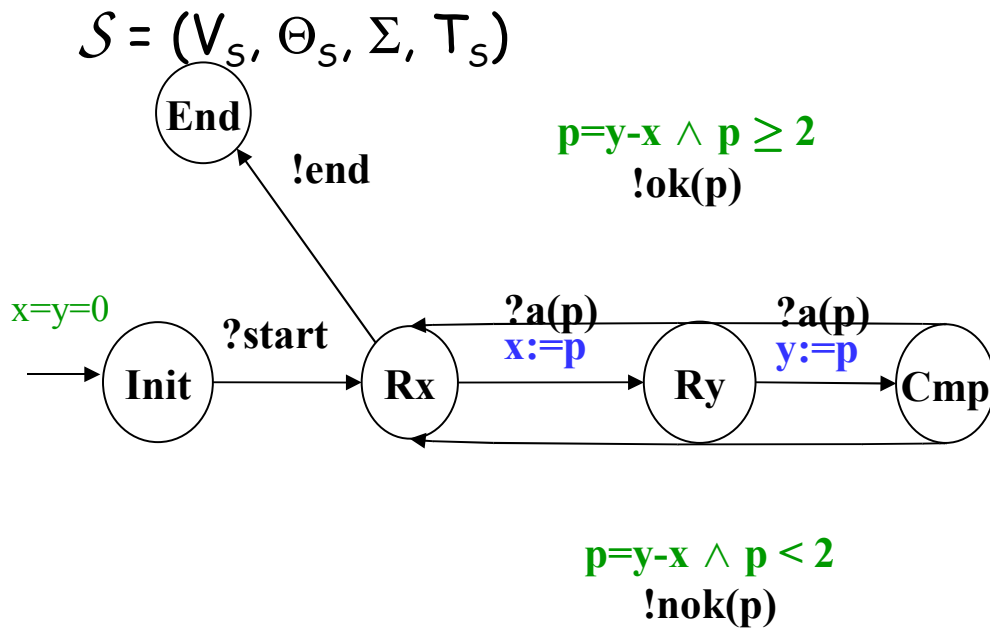
2. Conformance Testing Theory with ioco [Tretmans 96]

- Specification: known ioLTS S (semantics of an ioSTS)
- Implementation: **unknown** ioLTS I
- Conformance: $I \text{ ioco } S$: partial inclusion of $S\text{Tr}(I)$ in $S\text{Tr}(S)$
- Test cases : ioSTS TC + Verdicts
 - Execution: parallel composition $\Delta(I) \parallel TC$
 - Verdicts: TC may fail I
- Test generation: $\text{gen_test}: S \rightarrow TS = \{TC_1, TC_2, \dots\}$
Requested Properties of TS : may fail $\leftrightarrow \neg I \text{ ioco } S$
(soundness, limit exhaustiveness)

Simplification: an automata/language point of view

Conformance relation

**I ioco S $\triangleq \forall \sigma \in STr(S),$
Out($\Delta(I)$ after σ) \subseteq Out($\Delta(S)$ after σ)**



Conformant traces, e.g.
 $?start . ?a(4) . ?a(6) . !ok(2)$
 $?start . !end$
 $?start . ?start$
 (unspecified input allowed)

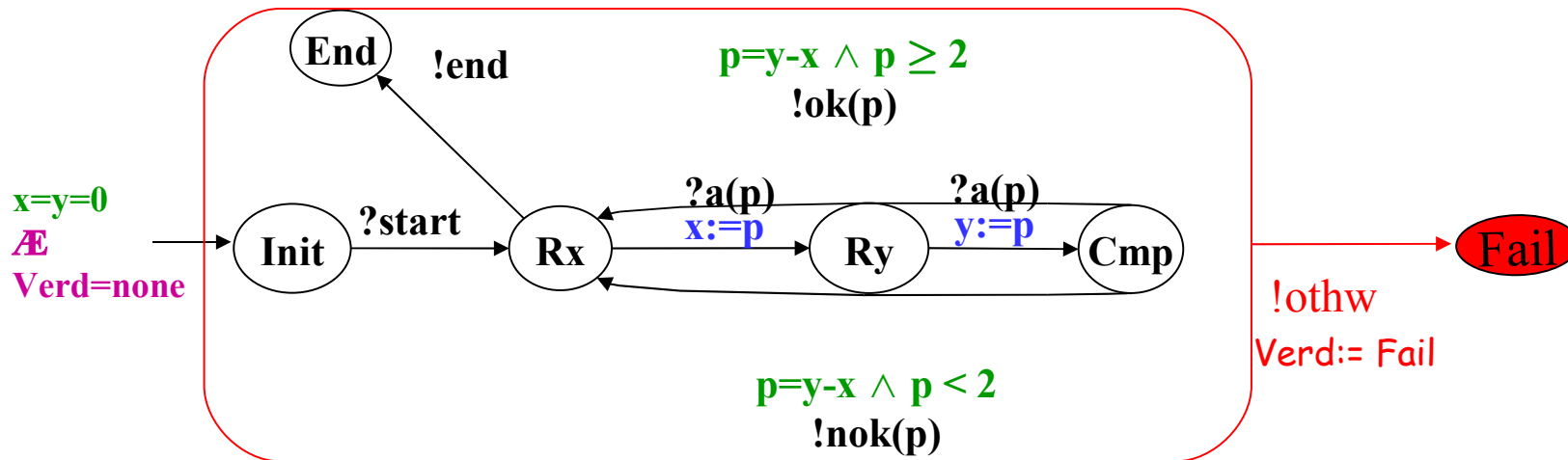
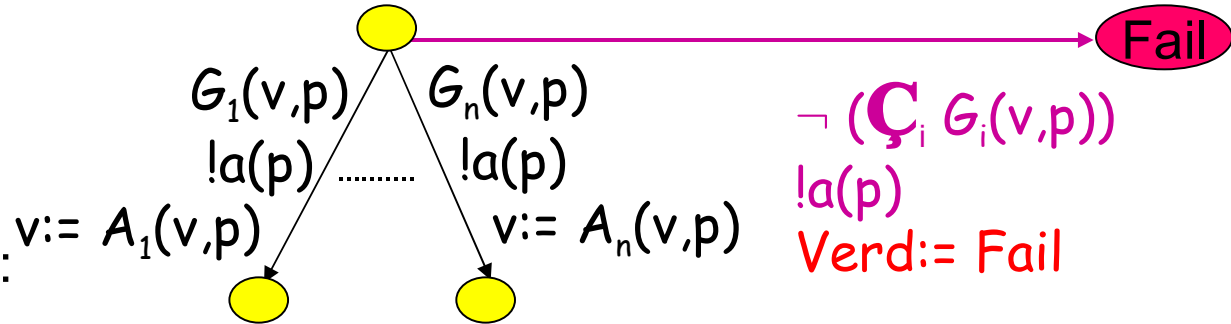
Non-conformant traces, e.g.
 $?start . ?a(5) . ?a(7) . !ok(3)$
 $?start . ?a(6) . ?a(8) . !nok(2)$

Prop: I ioco S $\Leftrightarrow STr(I) \dot{\Delta} [STr(S) . \Lambda_i^\delta \setminus STr(S)] = \emptyset$
 [non-conformant behaviours]

Canonical Tester $\text{Can}(S)$: observer of non-conformant behaviours

1. Add new variable Verd
with initial value none
i.e. $\Theta \text{AE Verd} = \text{none}$

2. \forall output $!a$, $\forall t$ carrying $!a$:



$$\text{STr}_{\text{Fail}}(\text{Can}(S)) = [\text{STr}(S). \Lambda_i^\delta \setminus \text{STr}(S)]$$

$$\Rightarrow \text{I ioco } S \Leftrightarrow \text{STr}(I) \dot{\wedge} \text{STr}_{\text{Fail}}(\text{Can}(S)) = \emptyset$$

Test cases, test execution, verdicts and properties

Test Case: deterministic ioSTS $TC = (V_{TC}, \Theta_{TC}, \Sigma, T_{TC})$

+ verdict boolean variables: **Fail**, **Pass**, **Inconc**, ...

plays the role of an observer delivering verdicts

$Tr_{Fail}(TC)$

Test suite: (infinite) set of test cases $TS = \{TC_1, TC_2, \dots\}$

Test execution: $TC \parallel \Delta(I)$ synchronization on common actions

Possible rejection of I by TC:

reachability of **Fail** in $TC \parallel \Delta(I)$ i.e.

TC may fail $I \triangleq STr(I) \dot{\wedge} Tr_{Fail}(TC) \neq \emptyset$

TS may fail I $\triangleq STr(I) \dot{\wedge} \bigwedge_{TC \in TS} Tr_{Fail}(TC) \neq \emptyset$

Test suite properties

Possible rejection by a TC should correspond to non-conformance and vice-versa

$$\neg \text{TS may fail } I \Leftrightarrow S\text{Tr}(I) \dot{\wedge}_{TC \in \text{TS}} \text{Tr}_{\text{Fail}}(TC) = \emptyset$$

$$I \text{ ioco } S \Leftrightarrow S\text{Tr}(I) \dot{\wedge} \text{Tr}_{\text{Fail}}(\text{Can}(S)) = \emptyset$$

$$\text{TS is sound} \triangleq \forall I, (I \text{ ioco } S \Rightarrow \neg \text{TS may fail } I)$$

$$\Leftrightarrow \bigwedge_{TC \in \text{TS}} \text{Tr}_{\text{Fail}}(TC) \subseteq \text{Tr}_{\text{Fail}}(\text{Can}(S))$$

$$\text{TS is exhaustive} \triangleq \forall I, (\neg \text{TS may fail } I \Rightarrow I \text{ ioco } S)$$

$$\Leftrightarrow \bigwedge_{TC \in \text{TS}} \text{Tr}_{\text{Fail}}(TC) \supseteq \text{Tr}_{\text{Fail}}(\text{Can}(S))$$

3. Test selection for *ioSTS*

$TS = \{Can(S)\}$ is a sound and exhaustive test suite but

- has too many (infinite) behaviours
- does not allow to control the implementation during testing

⇒ Test selection

- renounce to exhaustiveness in practice,
- focus on some targetted behaviours of $Can(S)$
select a finite TS likely to discover non-conformances
- use test purposes

Test purposes

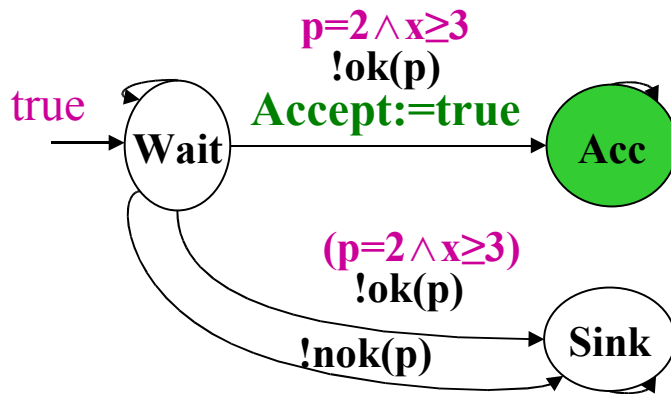
$$\mathcal{TP} = (V_S \cup V_{TP}, \Theta_{TP}, \Sigma, T_{TP})$$

Observer of actions and variables of S

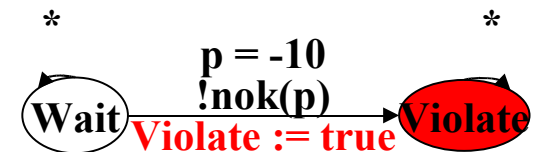
$$[a(p) : G(v_S, v_{TP}, p); v_{TP} := A(v_S, v_{TP}, p)] \in T_{TP}$$

Hyp : complete and deterministic

\mathcal{TP}_+ : reachability property

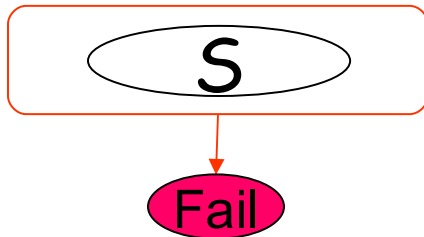


\mathcal{TP}_- : negation of safety property

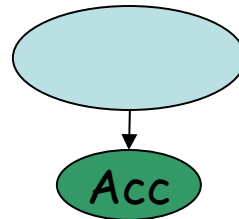


General principle

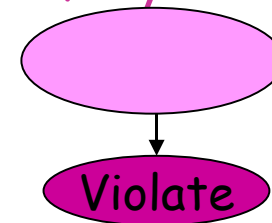
Can(S)
non-conformance
observer



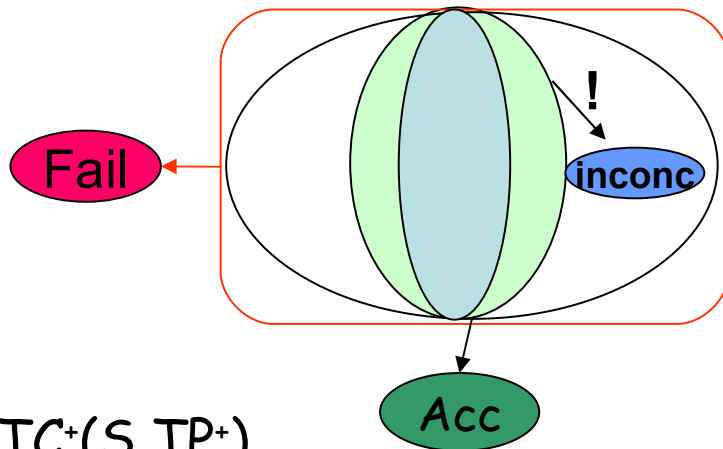
TP⁺
Reachability Observer



TP⁻
Safety Observer

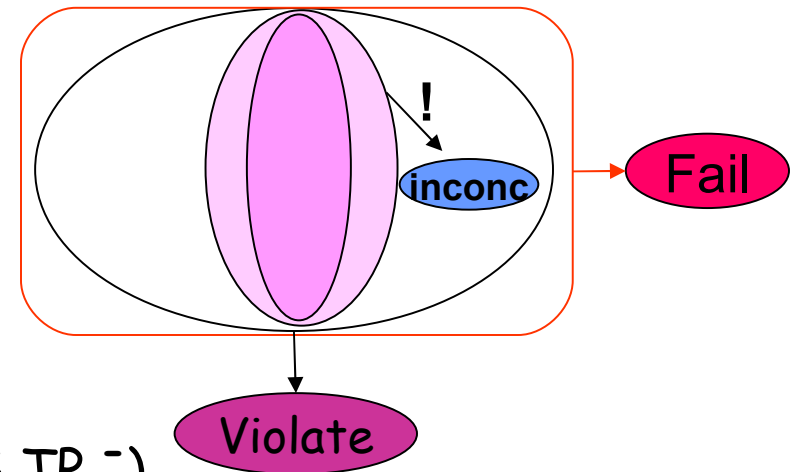


Can(S) × TP⁺:



TC⁺(S, TP⁺)
non-conf. and reach. observer

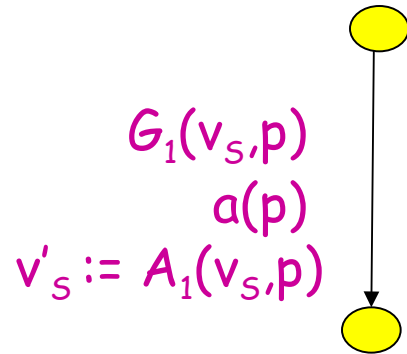
Can(S) × TP⁻:



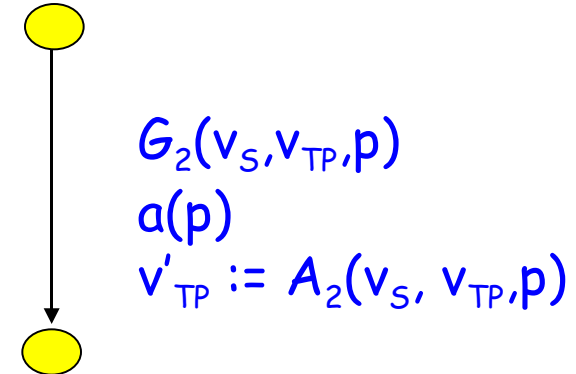
TC⁻(S, TP⁻)
non-conf. and safety observer

Syntactical product $Can(S) \times \mathcal{TP}$

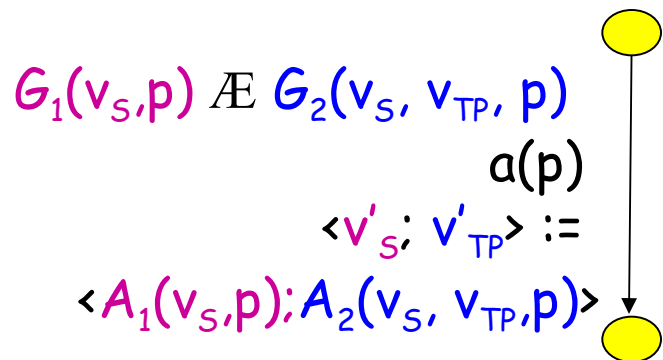
$$Can(S) = (V_A, \Theta_A, \Sigma, T_A)$$



$$\mathcal{TP} = (V_S \cup V_{TP}, \Theta_{TP}, \Sigma, T_{TP})$$



$$SP = Can(S) \times \mathcal{TP} = (V_S \cup V_{TP}, \Theta_S \dot{\wedge} \Theta_{TP}, \Sigma, T_{S \times TP})$$

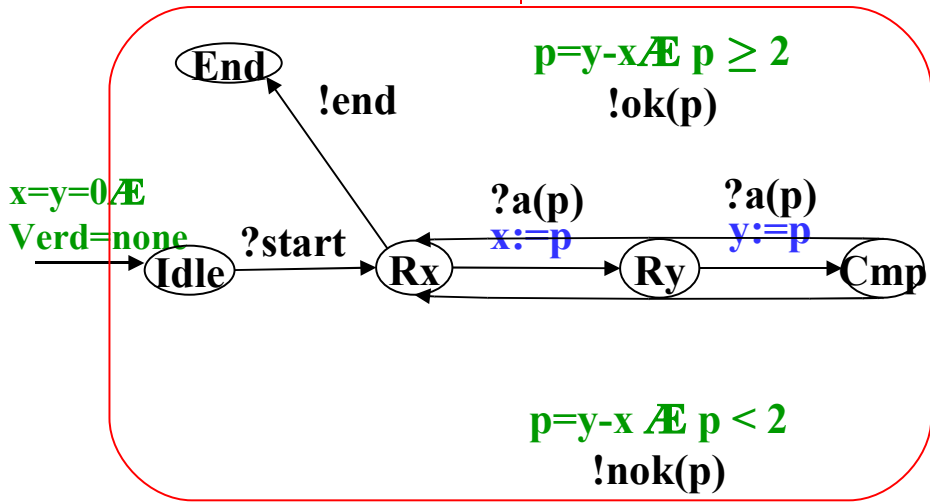


Syntactical product

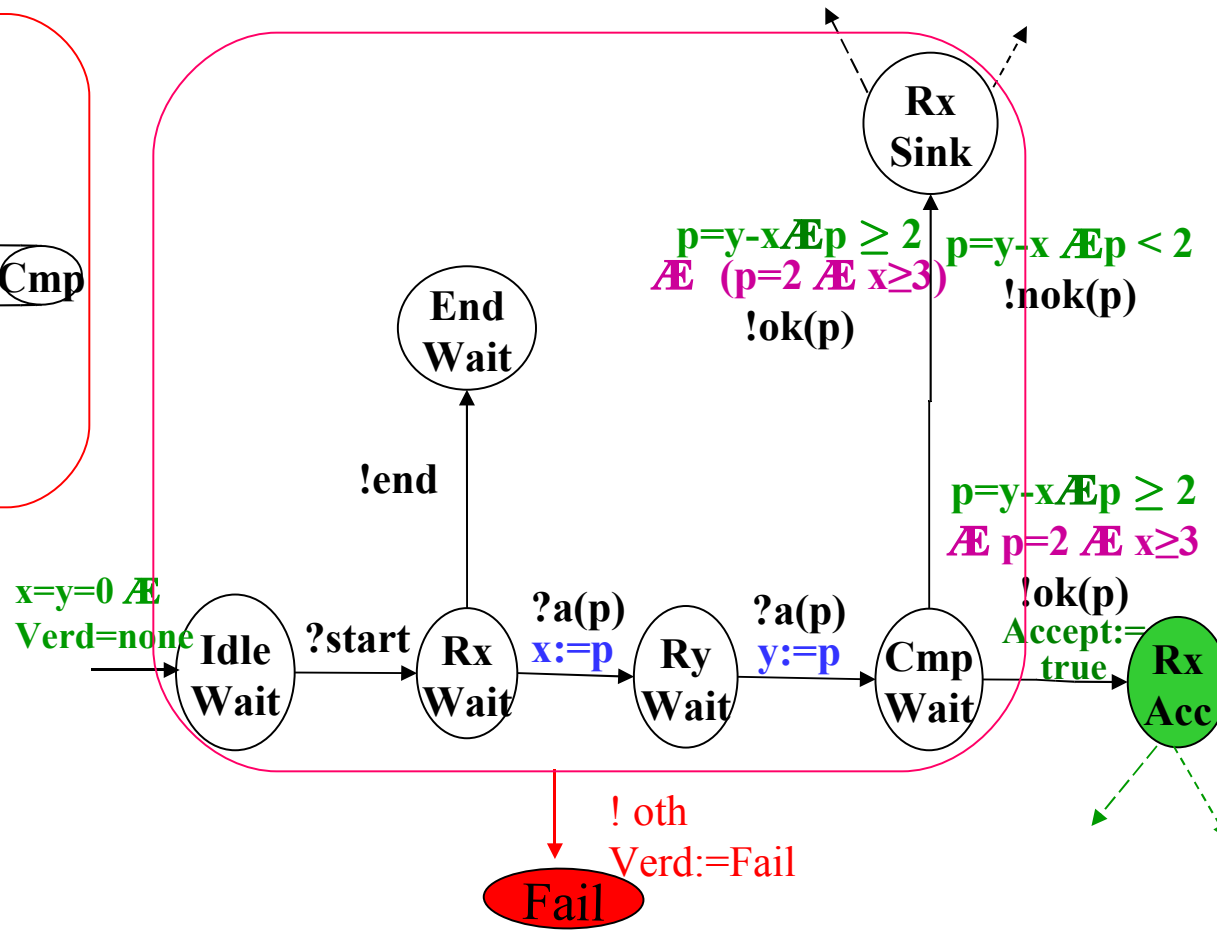
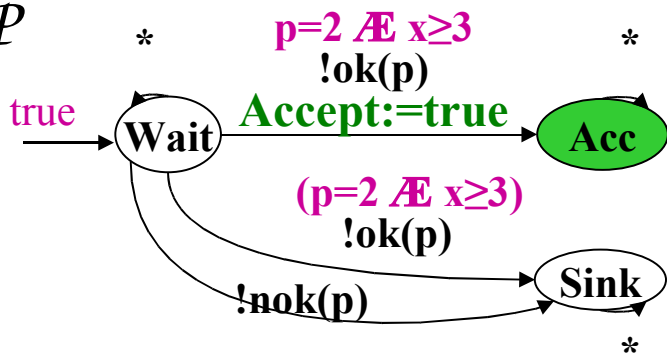
$Can(S)$



$$SP \triangleq Can(S) \times TP$$

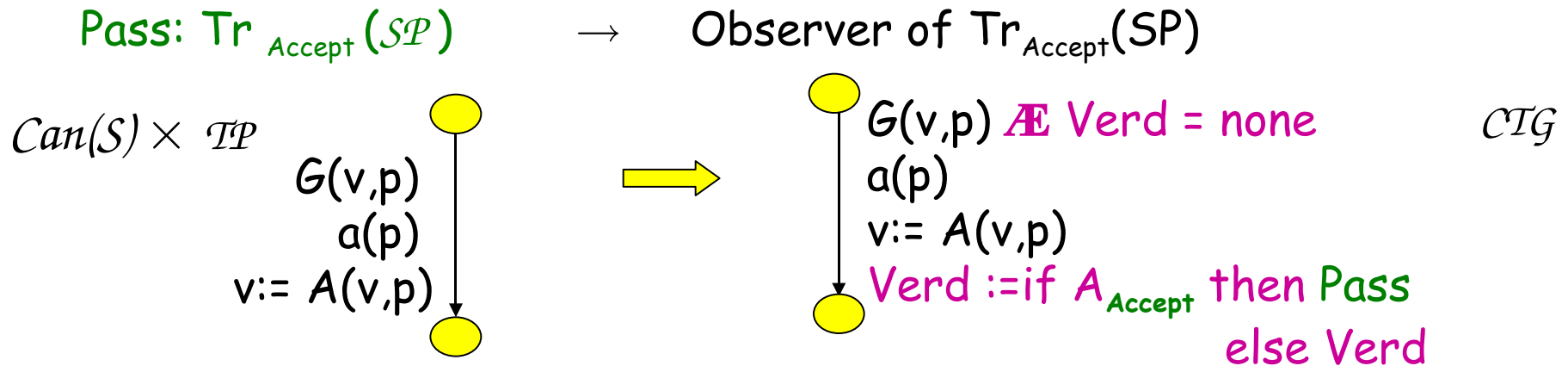


TP



Syntactical Test Selection (1)

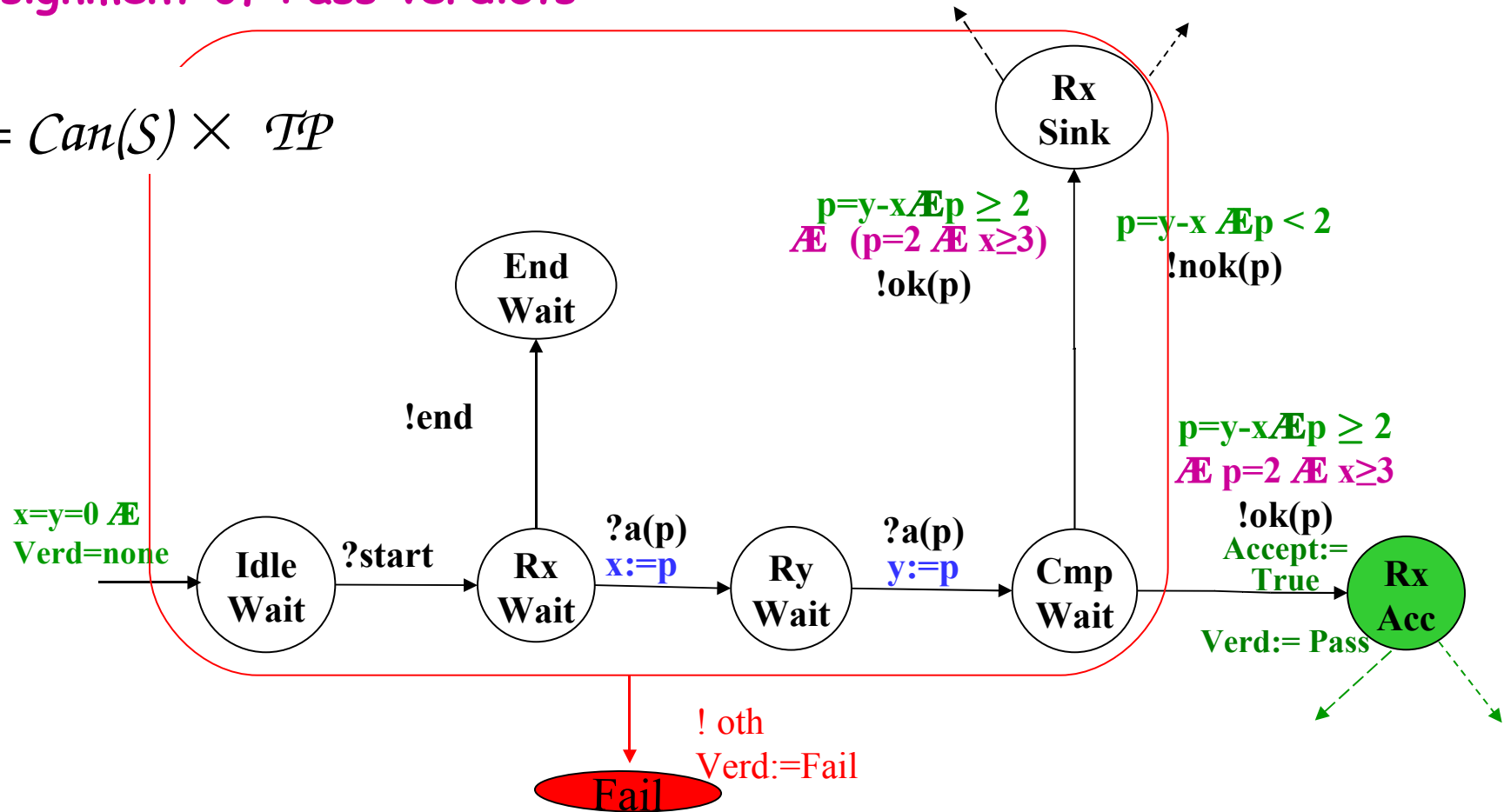
1. Assignment of Pass verdicts



Syntactical Test Selection (1)

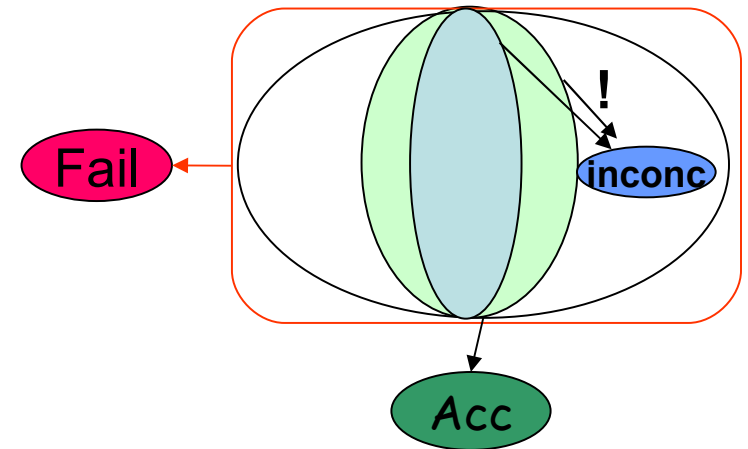
1. Assignment of Pass verdicts

$$SP = Can(S) \times TP$$



After product we get

- $\text{Tr}(SP) = \text{Tr}(\text{Can}(S))$
- $\text{Tr}_{\text{Fail}}(SP) = \text{Tr}_{\text{Fail}}(\text{Can}(S))$
- $\text{Tr}_{\text{Pass}}(SP) = \text{Tr}_{\text{Accept}}(TP) \dot{\wedge} \text{Tr}(S)$



SP is both a non-conformance and reachability observer
but has too much behaviours: $(\text{Tr}(\text{Can}(S)))$

Goal of selection:

focus on $\text{Tr}_{\text{Accept}}(TP) \dot{\wedge} \text{Tr}(S)$,

detect unfeasible traces to **Accept**

Amounts to compute $\text{co-reach}(\text{Accept})$

Undecidable \Rightarrow over-approximate

Syntactical Test Selection (2)

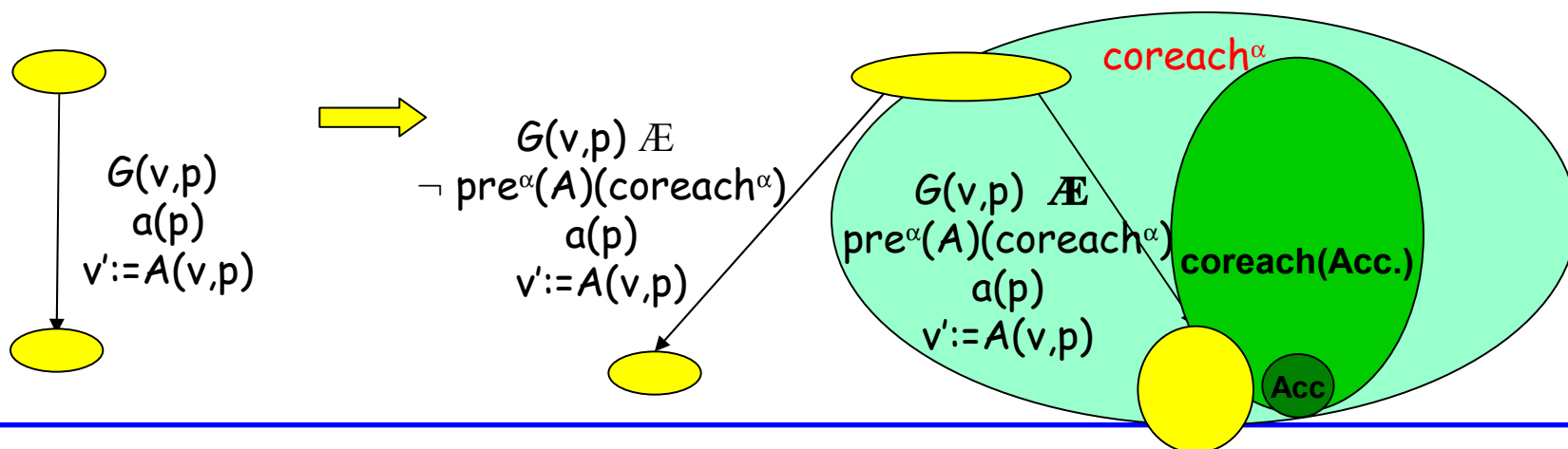
2. Selection and assignment of Inconc verdicts

$\text{coreach}(\text{Accept})$ not computable \Rightarrow compute over-approximation:

$$\text{coreach}^\alpha \supseteq \text{coreach}(\text{Accept})$$

$$\forall \text{ assignment } A, \text{pre}^\alpha(A) (\text{coreach}^\alpha) \supseteq \text{pre}(A) (\text{coreach}^\alpha)$$

Idea: $\text{pre}^\alpha(A) (\text{coreach}^\alpha) = \text{Nec. Cond. to go into } \text{coreach}^\alpha$
 $\neg \text{pre}^\alpha(A) (\text{coreach}^\alpha) = \text{Suf. Cond. to go outside } \text{coreach}^\alpha$
 $\subseteq \text{outside } \text{coreach}(\text{Accept})$

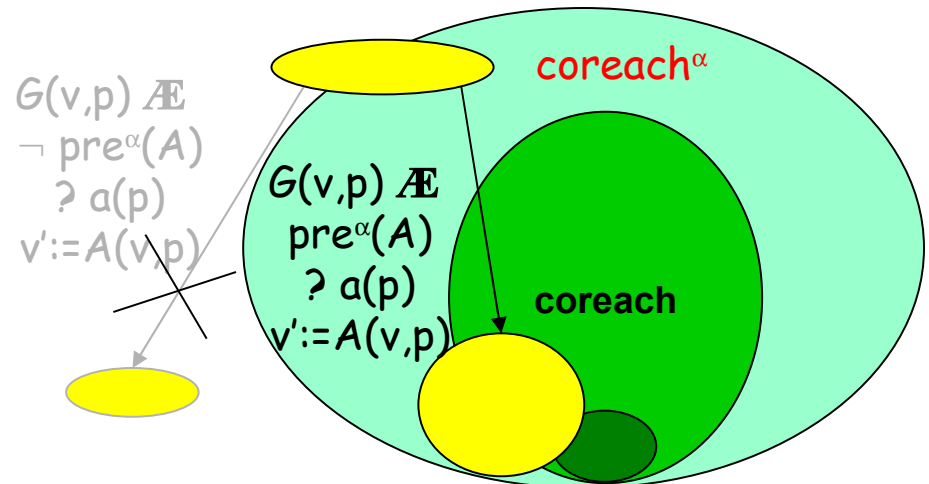


Syntactical test selection (3): guard strengthening

Rule for inputs of s :

keep conditions leading to coreach^α ,

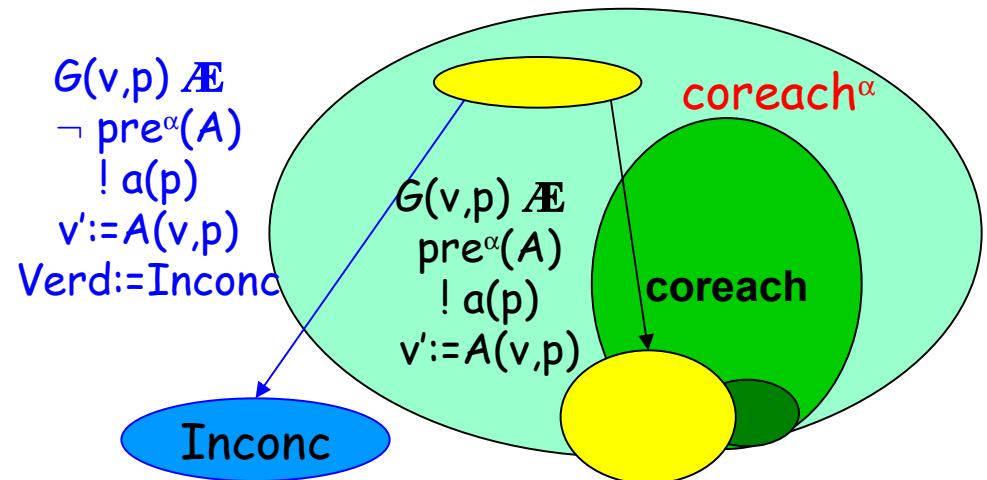
cut other ones (controllable):



Rule for outputs of s

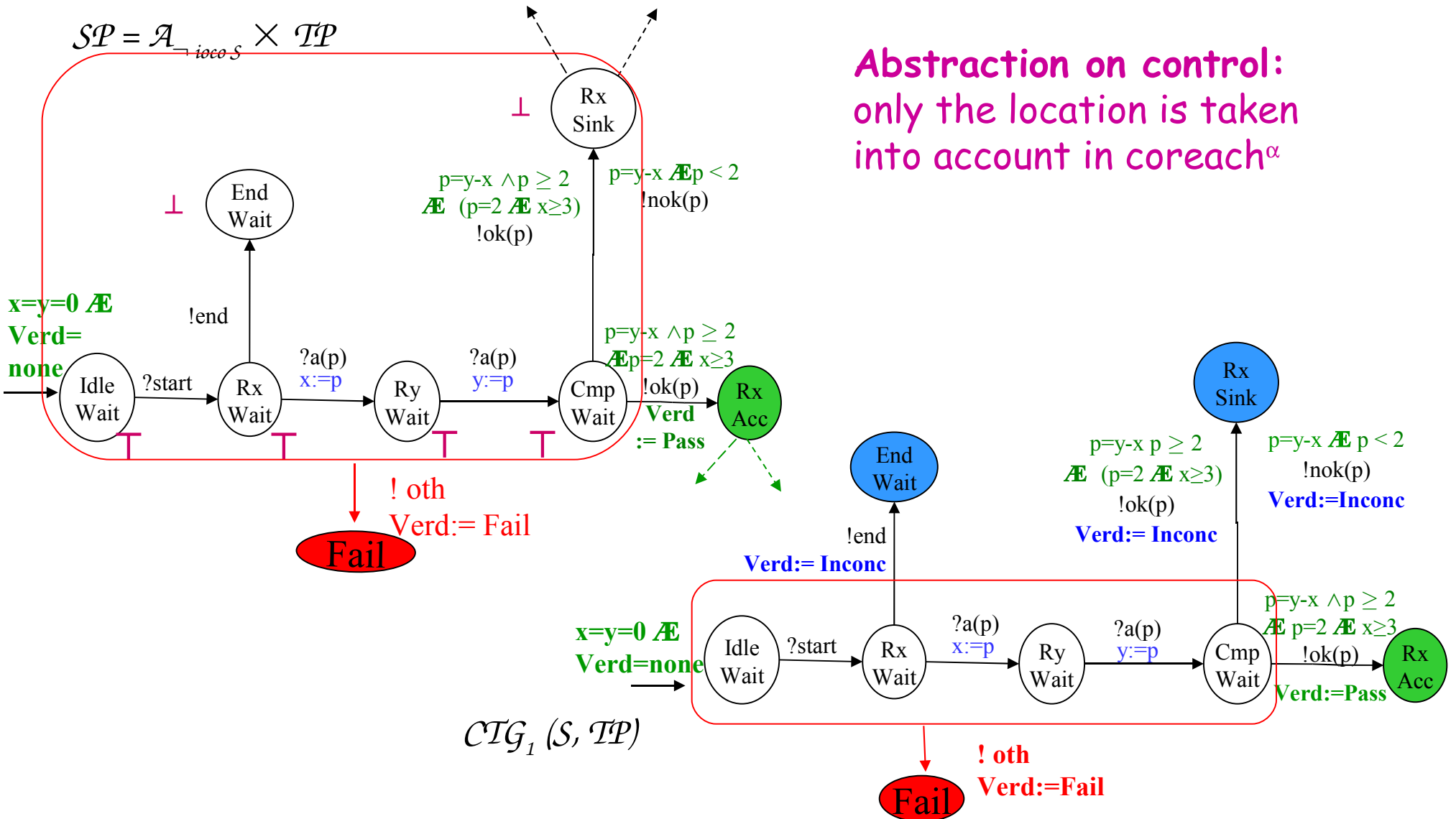
keep all conditions (uncontrollable),

those leading outside coreach^α
 produce **Inconc**:



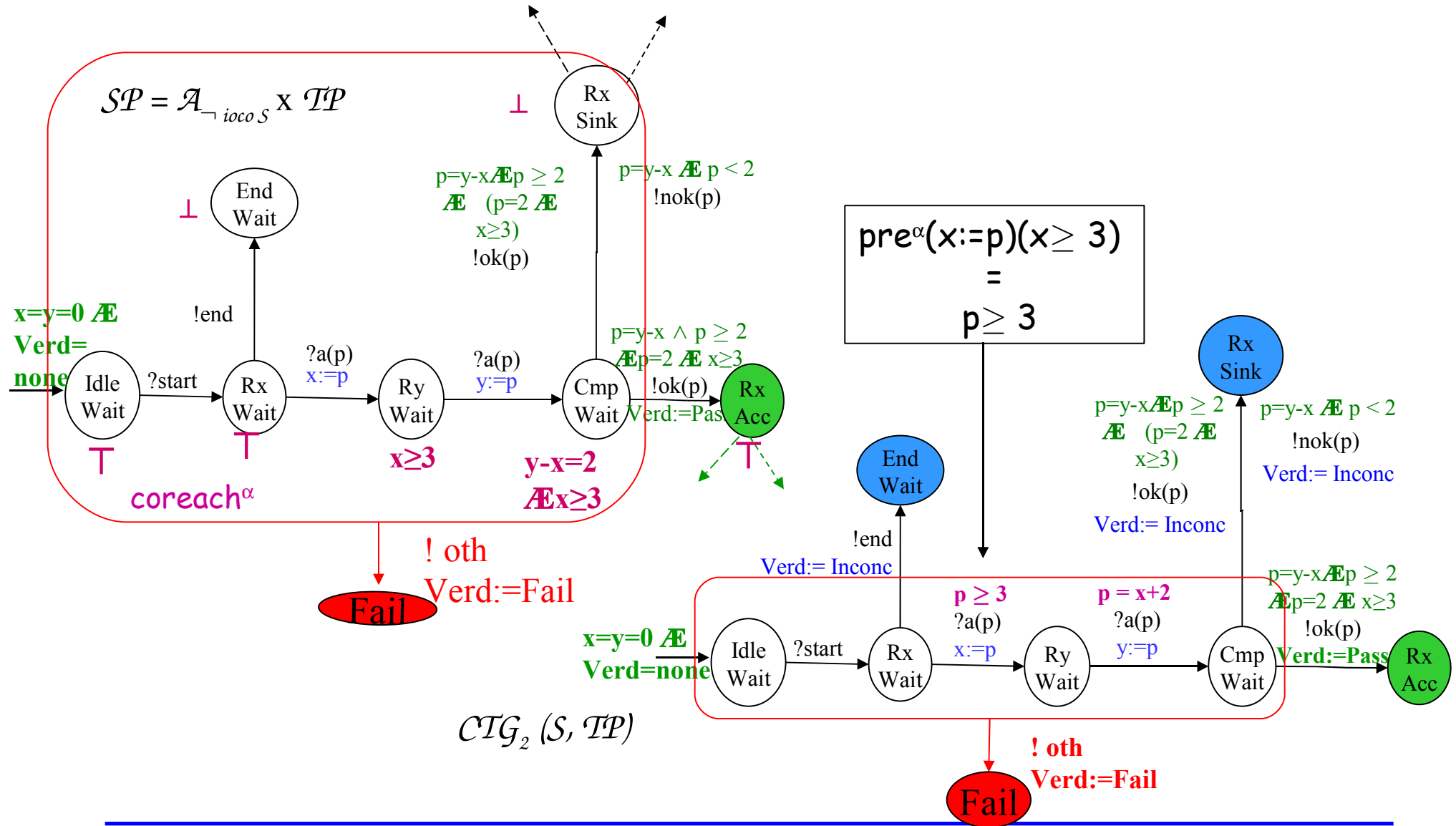
Test selection: example

1st over-approximation : control

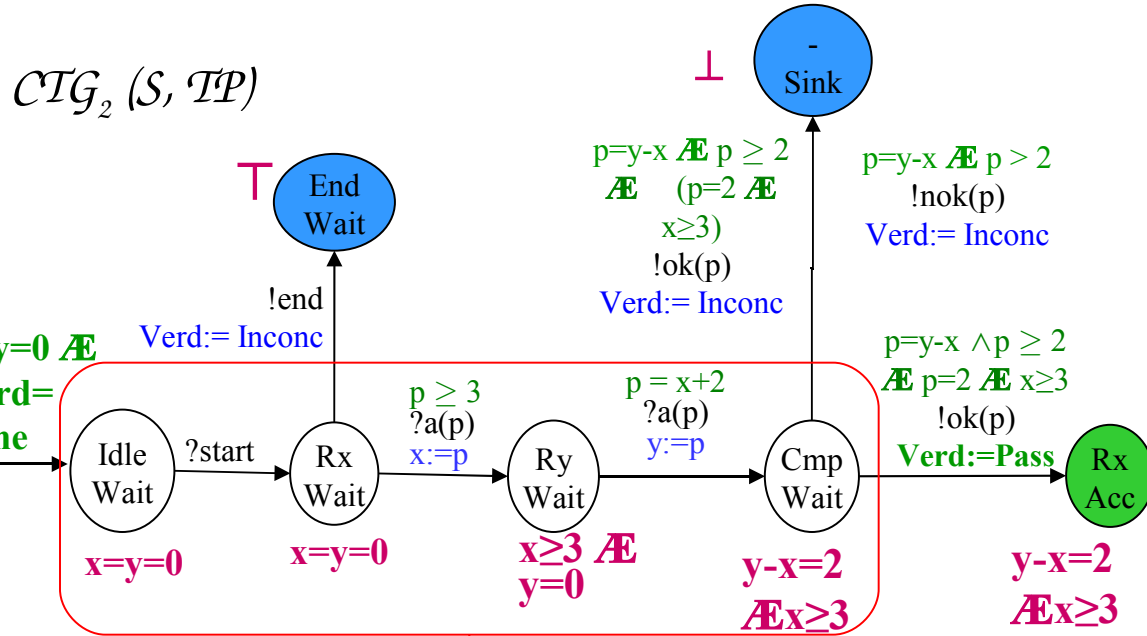


Test selection: example

2nd approximation computed by NBAC (convex polyhedra)

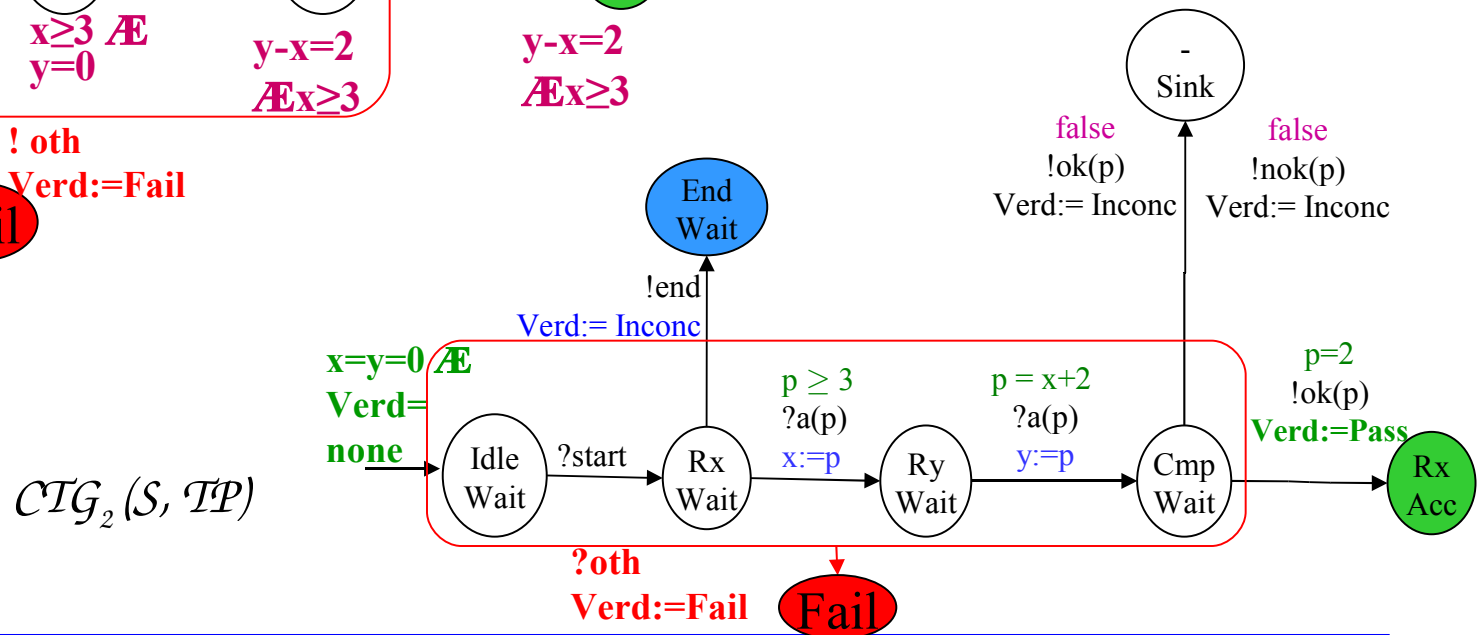


Simplification: over-approximation reach^α of $\text{reach}(\Theta)$



Simplify guards according to reach^α (false \Rightarrow cut)

NB: semantics is unchanged



Consequences of over-approximation on test cases

For two abstractions α_1 and α_2
 (e.g. α_1 : control vs α_2 : polyhedra)

$$\text{pre}^{\alpha_1}(A) (\text{coreach}^{\alpha_1}) \supseteq \text{pre}^{\alpha_2}(A) (\text{coreach}^{\alpha_2})$$

\Rightarrow

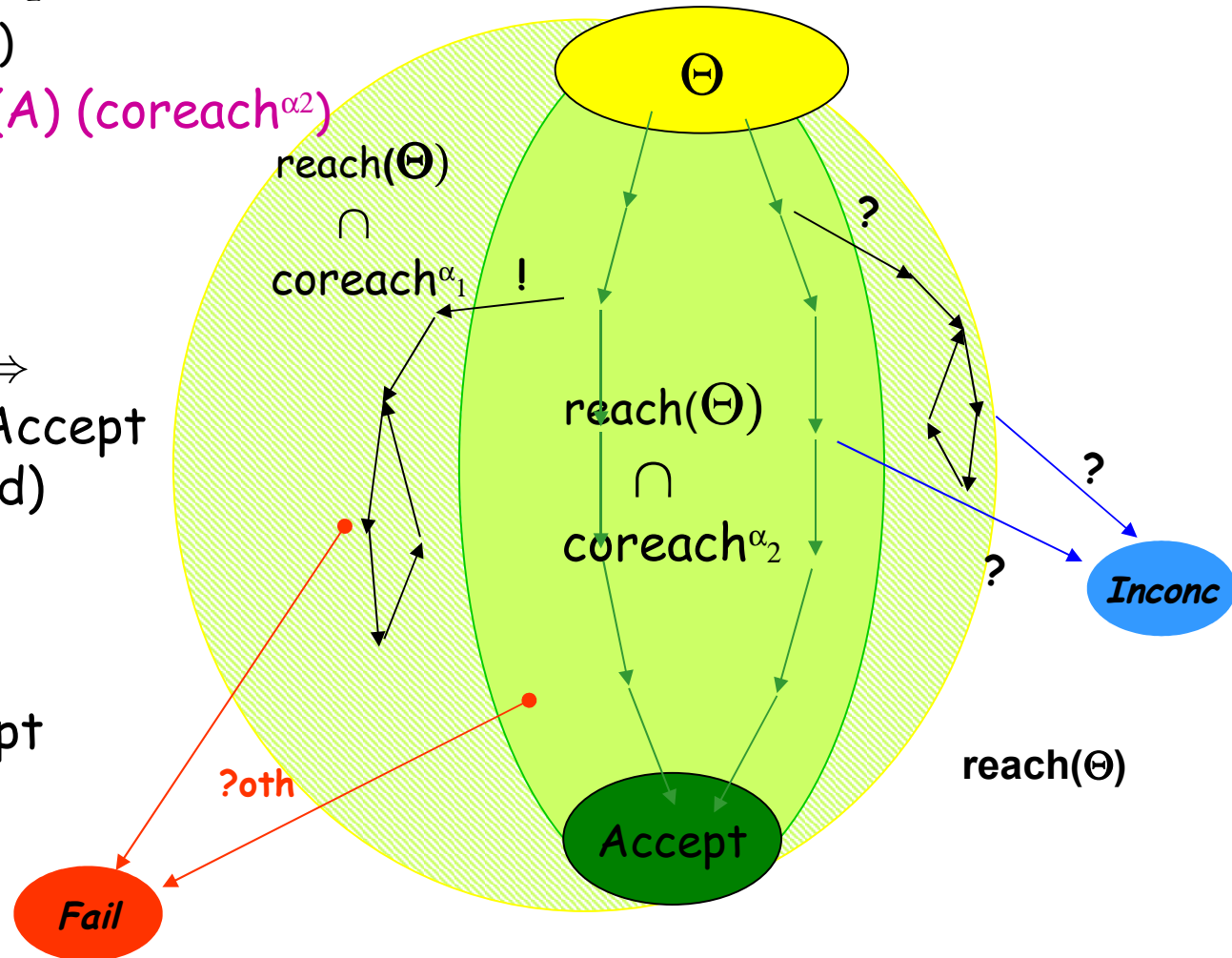
$$\text{Tr}(CTG_1) \supseteq \text{Tr}(CTG_2)$$

Less precise approximation \Rightarrow

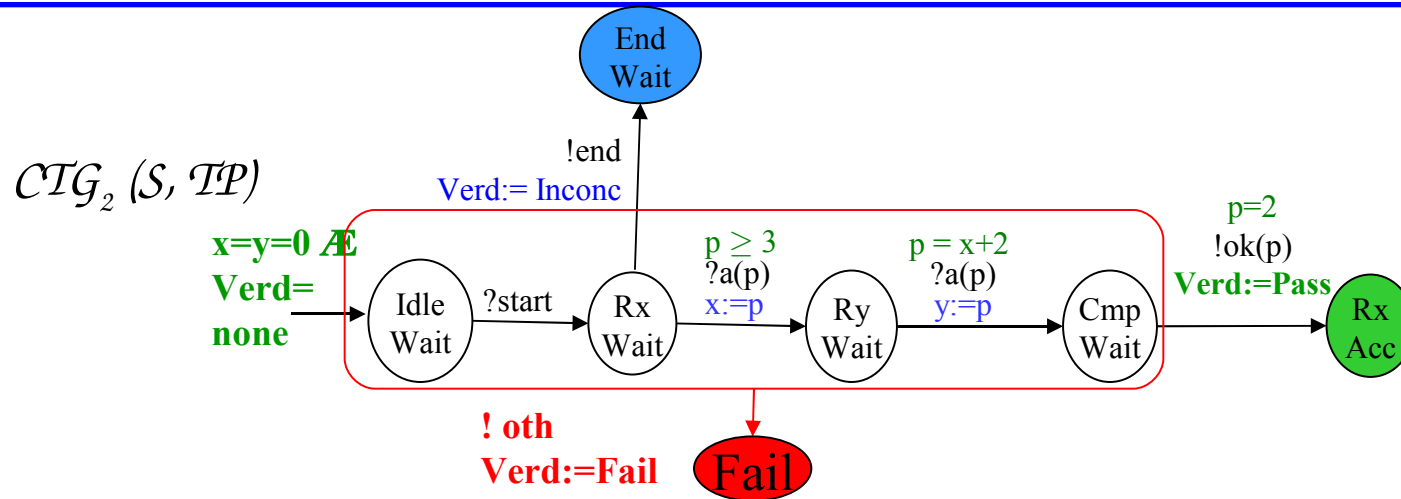
- More infeasible traces to Accept
- More fail verdicts (all sound)

Limit cases:

- exact analysis:
best guiding to Accept
- no analysis:
no guiding to Accept



Test execution



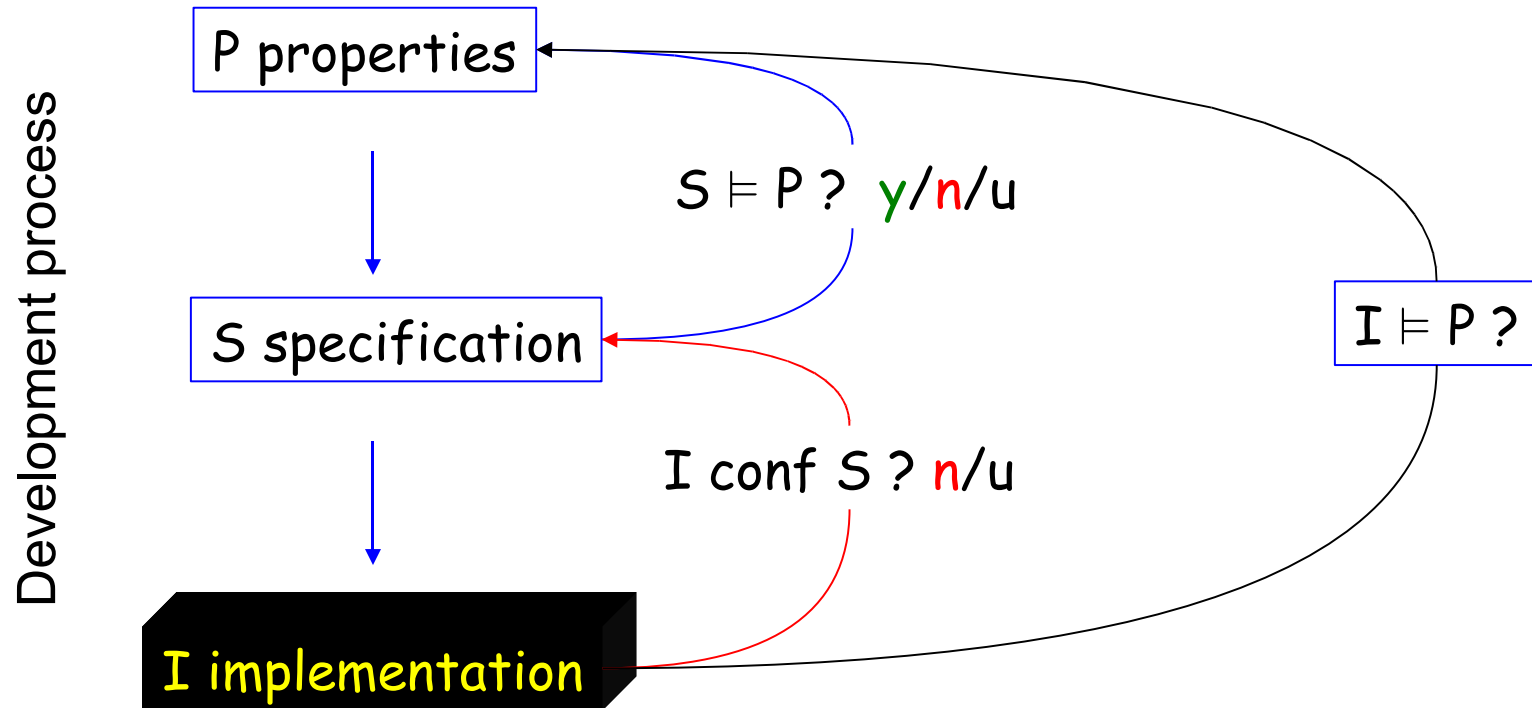
Inputs: $[? a(p) : G(v,p); v:=A(v,p)]$: v is known,
 choose π s.t. $G(v,\pi)$, by **constraint solving**
 send $a(\pi)$, assign $v:=A(v, \pi)$

Outputs: $[! a(p) : G(v,p); v:=A(v,p)]$: v is known,
 receive $a(\pi)$
 evaluate $G(v,\pi)$
 if true, assign $v:= A(v,\pi)$ (input complete)

?start . ?a(4) . ?a(6) . !ok(2) : **Pass**
 ?start . !end : **Inconc**

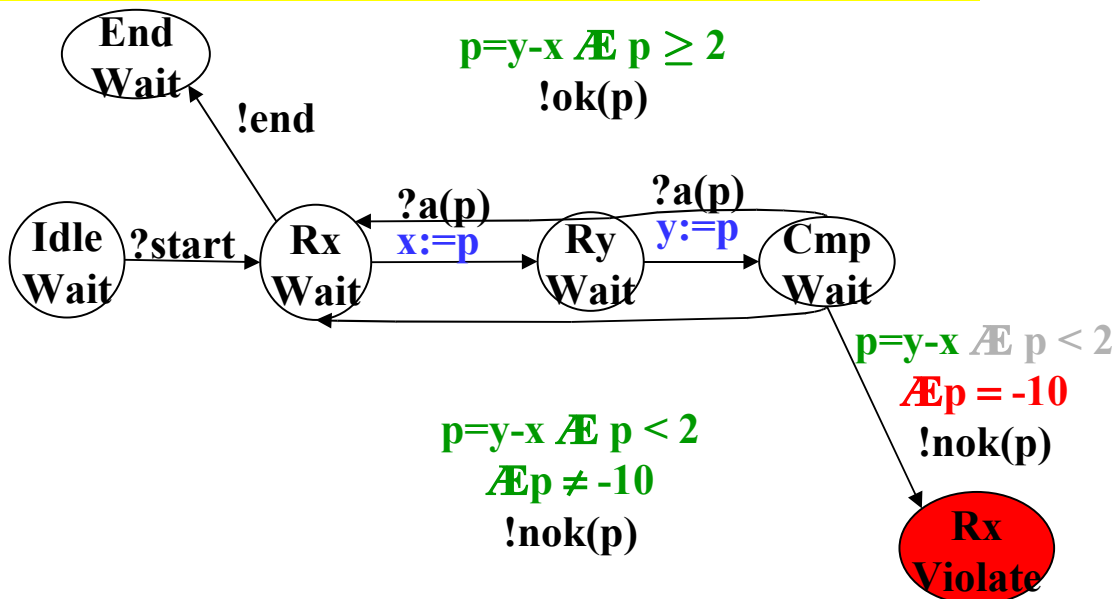
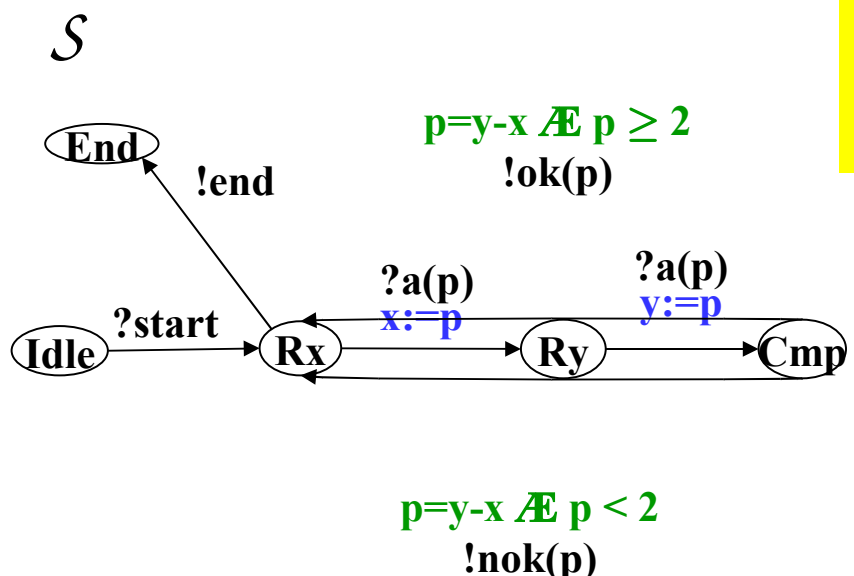
?start . ?a(5) . ?a(7) . !ok(3) : **Fail**
 ?start . ?a(6) . ?a(8) . !ok(2) : **Fail**

Verification and Testing

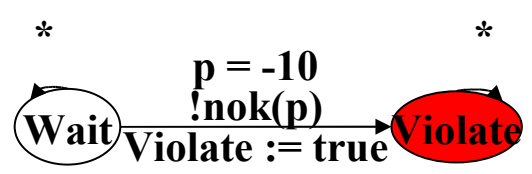


Model-checking a safety property

Model-checking $S \models P$? reduces to reachability in $S \times \mathcal{A}_{\neg P}$ (undecidable)

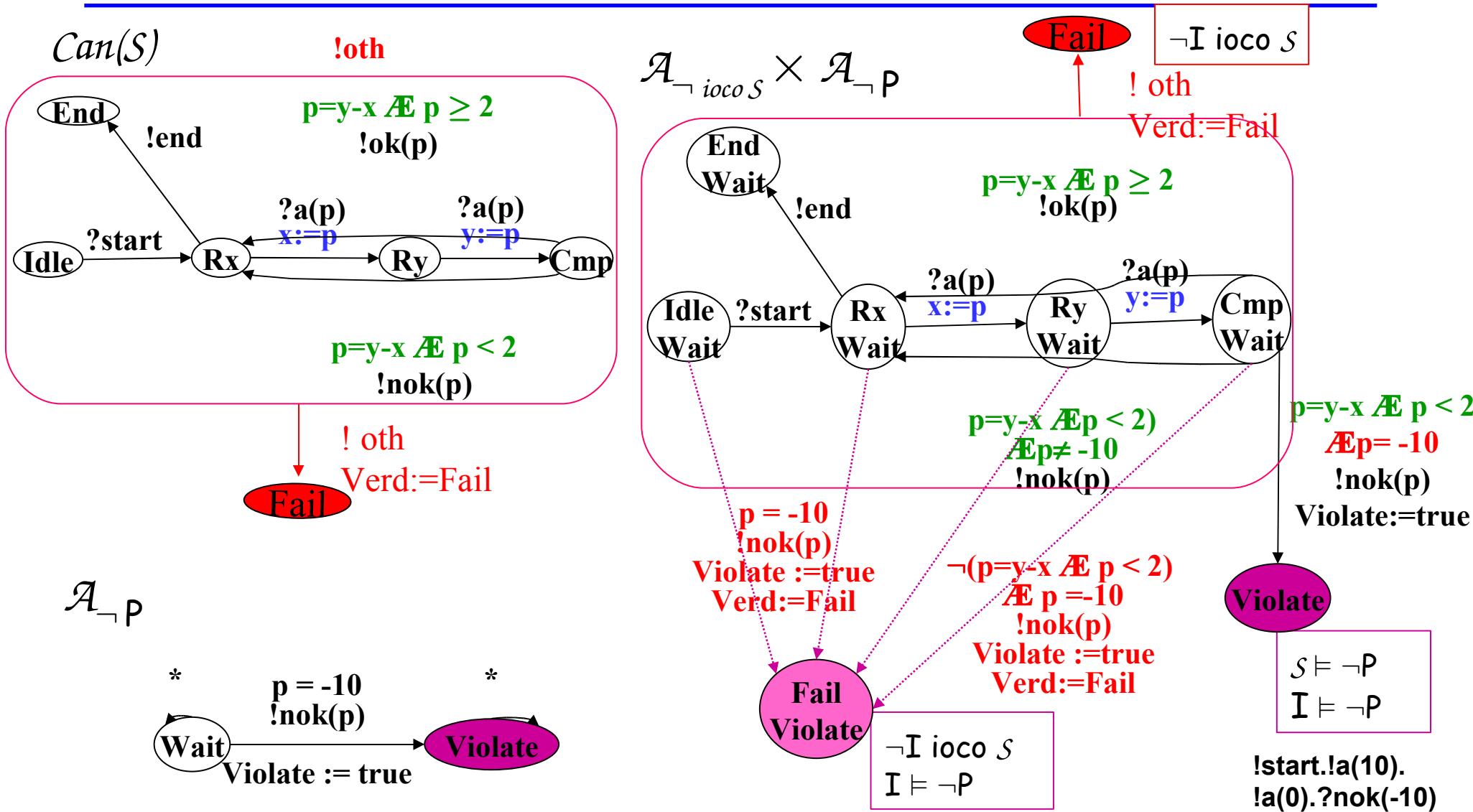


$\mathcal{TP} - = \mathcal{A}_{\neg P}$



$S \models \neg P : ?start.?a(10).?a(0).!nok(-10) \rightarrow (Rx, Violate)$
 With any abstraction $S^\alpha \models \neg P$? is **Yes**
 but $S^\alpha \models \neg P \not\Rightarrow S \models \neg P$
 Result of $S \models P$? could be **Unknown**

Test selection from a safety observer



Some links between Model-checking and Conformance Testing

- Test selection using model-checking :
 - S deter., controllable, P reachability: $TC \simeq$ counter-exple of $S \models \neg P$
[Engels et al. 97, Gargantini et al.99]
 - Extension to coverage using CTL [Hong et al.02] or observers [Blom et al.04]
 - Non-controllable case is more complex (this talk)
- Checking properties on the implementation
 - Black-box checking [Peled et al.] : learn I by experiment, model-check $I \models P$

Conclusion

Simplified and general framework for Ioco-based Test selection

- For finite ioLTS and infinite *ioSTS*
- Unified For **Reachability** and **Safety Observers**
- Using verification: coreachability analysis, over-approximations
- Completing verification (case of safety)

More research work needed for, e.g.

- Theories and algorithms for other models of reactive systems
e.g. with time, data, stack, probabilities ...and combinations
- Coverage : measures, selection
- Links with structural testing techniques
-