



# Artificial Intelligence 1: planning

Lecturer: Tom Lenaerts

Institut de Recherches Interdisciplinaires et de Développements  
en Intelligence Artificielle (IRIDIA)  
Université Libre de Bruxelles



## Planning

- The Planning problem
- Planning with State-space search
- Partial-order planning
- Planning graphs
- Planning with propositional logic
- Analysis of planning approaches

## What is Planning

- Generate sequences of actions to perform tasks and achieve objectives.
  - **States, actions and goals**
- Search for solution over abstract space of plans.
- Assists humans in practical applications
  - **design and manufacturing**
  - **military operations**
  - **games**
  - **space exploration**

## Difficulty of real world problems

- Assume a problem-solving agent using some search method ...
  - **Which actions are relevant?**
    - Exhaustive search vs. backward search
  - **What is a good heuristic functions?**
    - Good estimate of the cost of the state?
    - Problem-dependent vs, -independent
  - **How to decompose the problem?**
    - Most real-world problems are *nearly* decomposable.

## Planning language

- What is a good language?
  - **Expressive enough to describe a wide variety of problems.**
  - **Restrictive enough to allow efficient algorithms to operate on it.**
  - **Planning algorithm should be able to take advantage of the logical structure of the problem.**
- STRIPS and ADL

## General language features

- Representation of states
  - **Decompose the world in logical conditions and represent a state as a *conjunction of positive literals*.**
    - Propositional literals: *Poor*  $\wedge$  *Unknown*
    - FO-literals (grounded and function-free): *At(Plane1, Melbourne)*  $\wedge$  *At(Plane2, Sydney)*
  - **Closed world assumption**
- Representation of goals
  - **Partially specified state and represented as a *conjunction of positive ground literals***
  - **A goal is *satisfied* if the state contains all literals in goal.**

## General language features

### ■ Representations of actions

#### □ **Action = PRECOND + EFFECT**

*Action*(Fly(*p*,*from*, *to*),

*PRECOND*:  $At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

*EFFECT*:  $\neg At(p,from) \wedge At(p,to)$

#### = **action schema (p, from, to need to be instantiated)**

- Action name and parameter list
- Precondition (conj. of function-free literals)
- Effect (conj of function-free literals and P is True and not P is false)

#### □ **Add-list vs delete-list in Effect**

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## Language semantics?

### ■ How do actions affect states?

#### □ **An action is applicable in any state that satisfies the precondition.**

#### □ **For FO action schema applicability involves a substitution $\theta$ for the variables in the PRECOND.**

$At(P1,JFK) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$

Satisfies :  $At(p,from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

With  $\theta = \{p/P1, from/JFK, to/SFO\}$

Thus the action is applicable.

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## Language semantics?

- The result of executing action  $a$  in state  $s$  is the state  $s'$

- **$s'$  is same as  $s$  except**

- Any positive literal  $P$  in the effect of  $a$  is added to  $s'$
- Any negative literal  $\neg P$  is removed from  $s'$

$At(P1,SFO) \wedge At(P2,SFO) \wedge Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge$   
 $Airport(SFO)$

- **STRIPS assumption: (avoids representational frame problem)**

*every literal NOT in the effect remains unchanged*

## Expressiveness and extensions

- STRIPS is simplified
  - **Important limit: function-free literals**
  - **Allows for propositional representation**
- Function symbols lead to infinitely many states and actions
- Recent extension: Action Description language (ADL)

$Action(Fly(p:Plane, from: Airport, to: Airport),$   
 $PRECOND: At(p,from) \wedge (from \neq to)$   
 $EFFECT: \neg At(p,from) \wedge At(p,to)$

Standardization : *Planning domain definition language (PDDL)*

## Example: air cargo transport

*Init*( $At(C1, SFO) \wedge At(C2, JFK) \wedge At(P1, SFO) \wedge At(P2, JFK) \wedge Cargo(C1) \wedge Cargo(C2) \wedge$   
 $Plane(P1) \wedge Plane(P2) \wedge Airport(JFK) \wedge Airport(SFO)$ )

*Goal*( $At(C1, JFK) \wedge At(C2, SFO)$ )

*Action*(*Load*( $c, p, a$ ))

PRECOND:  $At(c, a) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT:  $\neg At(c, a) \wedge In(c, p)$

*Action*(*Unload*( $c, p, a$ ))

PRECOND:  $In(c, p) \wedge At(p, a) \wedge Cargo(c) \wedge Plane(p) \wedge Airport(a)$

EFFECT:  $At(c, a) \wedge \neg In(c, p)$

*Action*(*Fly*( $p, from, to$ ))

PRECOND:  $At(p, from) \wedge Plane(p) \wedge Airport(from) \wedge Airport(to)$

EFFECT:  $\neg At(p, from) \wedge At(p, to)$

[*Load*( $C1, P1, SFO$ ), *Fly*( $P1, SFO, JFK$ ), *Load*( $C2, P2, JFK$ ), *Fly*( $P2, JFK, SFO$ )]

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## Example: Spare tire problem

*Init*( $At(Flat, Axle) \wedge At(Spare, trunk)$ )

*Goal*( $At(Spare, Axle)$ )

*Action*(*Remove*( $Spare, Trunk$ ))

PRECOND:  $At(Spare, Trunk)$

EFFECT:  $\neg At(Spare, Trunk) \wedge At(Spare, Ground)$

*Action*(*Remove*( $Flat, Axle$ ))

PRECOND:  $At(Flat, Axle)$

EFFECT:  $\neg At(Flat, Axle) \wedge At(Flat, Ground)$

*Action*(*PutOn*( $Spare, Axle$ ))

PRECOND:  $At(Spare, Ground) \wedge \neg At(Flat, Axle)$

EFFECT:  $At(Spare, Axle) \wedge \neg At(Spare, Ground)$

*Action*(*LeaveOvernight*)

PRECOND:

EFFECT:  $\neg At(Spare, Ground) \wedge \neg At(Spare, Axle) \wedge \neg At(Spare, trunk) \wedge \neg At(Flat, Ground) \wedge \neg At(Flat, Axle)$

This example goes beyond STRIPS: negative literal in pre-condition (ADL description)

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## Example: Blocks world

*Init*( $On(A, Table) \wedge On(B, Table) \wedge On(C, Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(B) \wedge Clear(C)$ )

*Goal*( $On(A, B) \wedge On(B, C)$ )

*Action*(*Move*( $b, x, y$ ))

PRECOND:  $On(b, x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge (b \neq x) \wedge (b \neq y) \wedge (x \neq y)$

EFFECT:  $On(b, y) \wedge Clear(x) \wedge \neg On(b, x) \wedge \neg Clear(y)$

*Action*(*MoveToTable*( $b, x$ ))

PRECOND:  $On(b, x) \wedge Clear(b) \wedge Block(b) \wedge (b \neq x)$

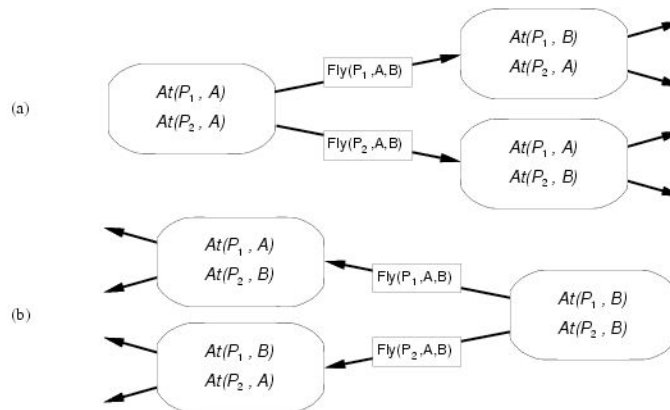
EFFECT:  $On(b, Table) \wedge Clear(x) \wedge \neg On(b, x)$

Spurious actions are possible: *Move*(B,C,C)

## Planning with state-space search

- Both forward and backward search possible
- Progression planners
  - **forward state-space search**
  - **Consider the effect of all possible actions in a given state**
- Regression planners
  - **backward state-space search**
  - **To achieve a goal, what must have been true in the previous state.**

## Progression and regression



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## Progression algorithm

- Formulation as state-space search problem:
  - **Initial state = initial state of the planning problem**
    - Literals not appearing are false
  - **Actions = those whose preconditions are satisfied**
    - Add positive effects, delete negative
  - **Goal test = does the state satisfy the goal**
  - **Step cost = each action costs 1**
- No functions ... any graph search that is complete is a complete planning algorithm.
- Inefficient: (1) irrelevant action problem (2) good heuristic required for efficient search

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## Regression algorithm

- How to determine predecessors?
  - **What are the states from which applying a given action leads to the goal?**
    - Goal state =  $At(C1, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$
    - Relevant action for first conjunct:  $Unload(C1,p,B)$
    - Works only if pre-conditions are satisfied.
    - Previous state =  $In(C1, p) \wedge At(p, B) \wedge At(C2, B) \wedge \dots \wedge At(C20, B)$
    - Subgoal  $At(C1,B)$  should not be present in this state.
- Actions must not undo desired literals (consistent)
- Main advantage: only relevant actions are considered.
  - **Often much lower branching factor than forward search.**

## Regression algorithm

- General process for predecessor construction
  - **Give a goal description G**
  - **Let A be an action that is relevant and consistent**
  - **The predecessors is as follows:**
    - Any positive effects of A that appear in G are deleted.
    - Each precondition literal of A is added , unless it already appears.
- Any standard search algorithm can be added to perform the search.
- Termination when predecessor satisfied by initial state.
  - **In FO case, satisfaction might require a substitution.**

## Heuristics for state-space search

- Neither progression or regression are very efficient without a good heuristic.
  - **How many actions are needed to achieve the goal?**
  - **Exact solution is NP hard, find a good estimate**
- Two approaches to find admissible heuristic:
  - **The optimal solution to the relaxed problem.**
    - Remove all preconditions from actions
  - **The subgoal independence assumption:**
    - The cost of solving a conjunction of subgoals is approximated by the sum of the costs of solving the subproblems independently.

## Partial-order planning

- Progression and regression planning are *totally ordered plan search* forms.
  - **They cannot take advantage of problem decomposition.**
    - Decisions must be made on how to sequence actions on all the subproblems
- Least commitment strategy:
  - **Delay choice during search**

# Shoe example

```

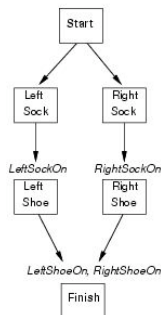
Goal(RightShoeOn ^ LeftShoeOn)
Init()
Action(RightShoe, PRECOND: RightSockOn
      EFFECT: RightShoeOn)
Action(RightSock, PRECOND:
      EFFECT: RightSockOn)
Action(LeftShoe, PRECOND: LeftSockOn
      EFFECT: LeftShoeOn)
Action(LeftSock, PRECOND:
      EFFECT: LeftSockOn)
    
```

Planner: combine two action sequences (1)leftsock, leftshoe  
 (2)rightsock, rightshoe

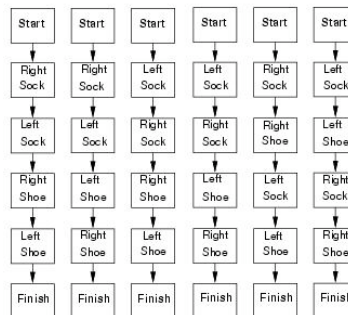
# Partial-order planning

- Any planning algorithm that can place two actions into a plan without which comes first is a POL.

Partial Order Plan:



Total Order Plans:



## POL as a search problem

- States are (mostly unfinished) plans.
  - **The empty plan contains only start and finish actions.**
- Each plan has 4 components:
  - **A set of actions (steps of the plan)**
  - **A set of ordering constraints:  $A < B$** 
    - Cycles represent contradictions.
  - **A set of causal links  $A \xrightarrow{p} B$** 
    - The plan may not be extended by adding a new action C that conflicts with the causal link. (if the effect of C is  $\neg p$  and if C could come after A and before B)
  - **A set of open preconditions.**
    - If precondition is not achieved by action in the plan.

## POL as a search problem

- A plan is *consistent* iff there are no cycles in the ordering constraints and no conflicts with the causal links.
- A consistent plan with no open preconditions is a *solution*.
- A partial order plan is executed by repeatedly choosing *any* of the possible next actions.
  - **This flexibility is a benefit in non-cooperative environments.**

## Solving POL

- Assume propositional planning problems:
  - **The initial plan contains *Start* and *Finish*, the ordering constraint  $Start < Finish$ , no causal links, all the preconditions in *Finish* are open.**
  - **Successor function :**
    - picks one open precondition  $p$  on an action  $B$  and
    - generates a successor plan for every possible consistent way of choosing action  $A$  that achieves  $p$ .
  - **Test goal**

## Enforcing consistency

- When generating successor plan:
  - **The causal link  $A \rightarrow p \rightarrow B$  and the ordering constraint  $A < B$  is added to the plan.**
    - If  $A$  is new also add  $start < A$  and  $A < B$  to the plan
  - **Resolve conflicts between new causal link and all existing actions**
  - **Resolve conflicts between action  $A$  (if new) and all existing causal links.**

## Process summary

- Operators on partial plans
  - Add link from existing plan to open precondition.
  - Add a step to fulfill an open condition.
  - Order one step w.r.t another to remove possible conflicts
- Gradually move from incomplete/vague plans to complete/correct plans
- Backtrack if an open condition is unachievable or if a conflict is unresolvable.

## Example: Spare tire problem

*Init*( $At(Flat, Axle) \wedge At(Spare, trunk)$ )

*Goal*( $At(Spare, Axle)$ )

*Action*(*Remove*(*Spare*, *Trunk*))

PRECOND:  $At(Spare, Trunk)$

EFFECT:  $\neg At(Spare, Trunk) \wedge At(Spare, Ground)$

*Action*(*Remove*(*Flat*, *Axle*))

PRECOND:  $At(Flat, Axle)$

EFFECT:  $\neg At(Flat, Axle) \wedge At(Flat, Ground)$

*Action*(*PutOn*(*Spare*, *Axle*))

PRECOND:  $At(Spare, Ground) \wedge \neg At(Flat, Axle)$

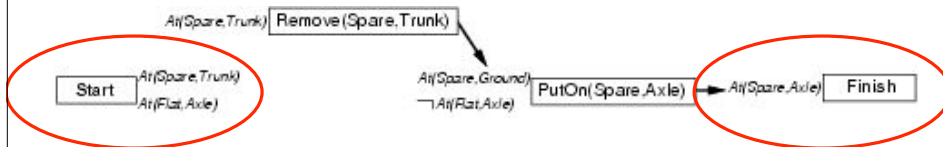
EFFECT:  $At(Spare, Axle) \wedge \neg Ar(Spare, Ground)$

*Action*(*LeaveOvernight*)

PRECOND:

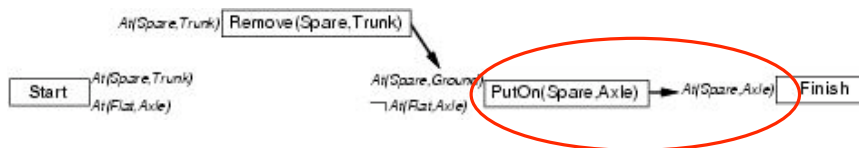
EFFECT:  $\neg At(Spare, Ground) \wedge \neg At(Spare, Axle) \wedge \neg At(Spare, trunk) \wedge \neg At(Flat, Ground) \wedge \neg At(Flat, Axle)$

## Solving the problem



- Initial plan: Start with EFFECTS and Finish with PRECOND.

## Solving the problem



- Initial plan: Start with EFFECTS and Finish with PRECOND.
- Pick an open precondition:  $At(Spare, Axle)$
- Only  $PutOn(Spare, Axle)$  is applicable
- Add causal link:  $PutOn(Spare, Axle) \xrightarrow{At(Spare, Axle)} Finish$
- Add constraint :  $PutOn(Spare, Axle) < Finish$

## Solving the problem



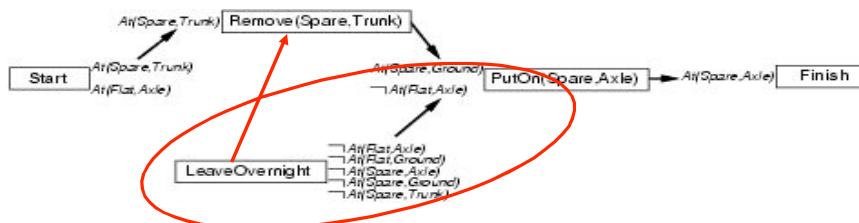
- Pick an open precondition:  $At(Spare, Ground)$
- Only  $Remove(Spare, Trunk)$  is applicable
- Add causal link:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- Add constraint :  $Remove(Spare, Trunk) < PutOn(Spare, Axle)$

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## Solving the problem



- Pick an open precondition:  $At(Spare, Ground)$
- $LeaveOverNight$  is applicable
- conflict:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- To resolve, add constraint :  $LeaveOverNight < Remove(Spare, Trunk)$

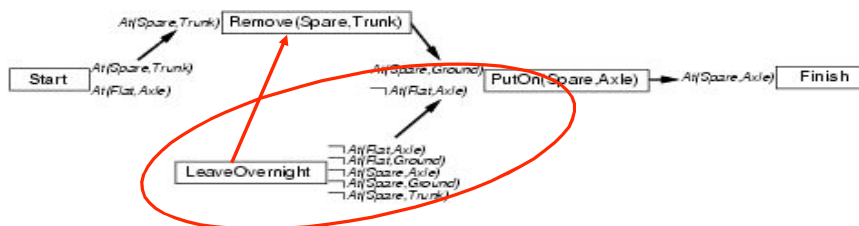
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## Solving the problem



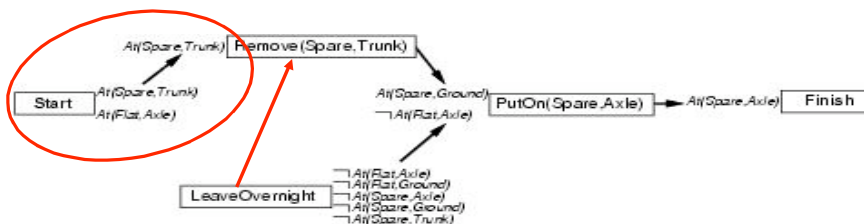
- Pick an open precondition:  $At(Spare, Ground)$
- $LeaveOverNight$  is applicable
- conflict:  $Remove(Spare, Trunk) \xrightarrow{At(Spare, Ground)} PutOn(Spare, Axle)$
- To resolve, add constraint :  $LeaveOverNight < Remove(Spare, Trunk)$
- Add causal link:
 
$$LeaveOverNight \xrightarrow{\neg At(Spare, Ground)} PutOn(Spare, Axle)$$

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## Solving the problem



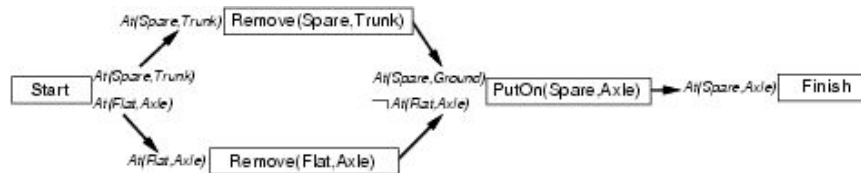
- Pick an open precondition:  $At(Spare, Trunk)$
- Only  $Start$  is applicable
- Add causal link:  $Start \xrightarrow{At(Spare, Trunk)} Remove(Spare, Trunk)$
- Conflict: of causal link with effect  $At(Spare, Trunk)$  in  $LeaveOverNight$ 
  - **No re-ordering solution possible.**
- backtrack

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## Solving the problem



- Remove *LeaveOverNight*, *Remove(Spare, Trunk)* and causal links
- Repeat step with *Remove(Spare, Trunk)*
- Add also *RemoveFlatAxle* and finish

## Some details ...

- What happens when a first-order representation that includes variables is used?
  - **Complicates the process of detecting and resolving conflicts.**
  - **Can be resolved by introducing inequality constraint.**
- CSP's most-constrained-variable constraint can be used for planning algorithms to select a PRECOND.

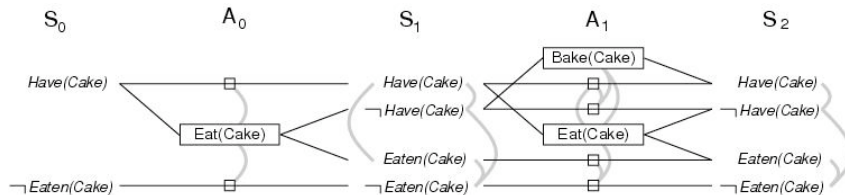
## Planning graphs

- Used to achieve better heuristic estimates.
  - **A solution can also directly extracted using GRAPHPLAN.**
- Consists of a sequence of levels that correspond to time steps in the plan.
  - **Level 0 is the initial state.**
  - **Each level consists of a set of literals and a set of actions.**
    - *Literals* = all those that *could* be true at that time step, depending upon the actions executed at the preceding time step.
    - *Actions* = all those actions that *could* have their preconditions satisfied at that time step, depending on which of the literals actually hold.

## Planning graphs

- “Could”?
  - **Records only a restricted subset of possible negative interactions among actions.**
- They work only for propositional problems.
- Example:
  - Init(Have(Cake))
  - Goal(Have(Cake)  $\wedge$  Eaten(Cake))
  - Action(Eat(Cake), PRECOND: Have(Cake)  
EFFECT:  $\neg$ Have(Cake)  $\wedge$  Eaten(Cake))
  - Action(Bake(Cake), PRECOND:  $\neg$  Have(Cake)  
EFFECT: Have(Cake))

## Cake example



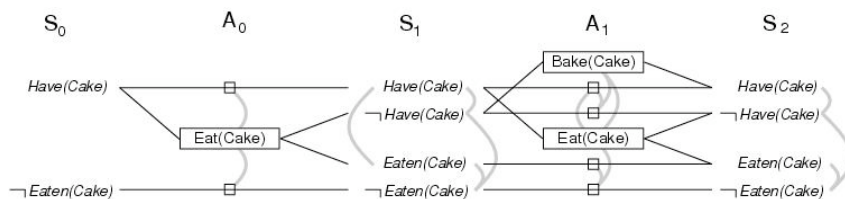
- Start at level  $S_0$  and determine action level  $A_0$  and next level  $S_1$ .
  - **$A_0 \gg$  all actions whose preconditions are satisfied in the previous level.**
  - **Connect precond and effect of actions  $S_0 \rightarrow S_1$**
  - **Inaction is represented by persistence actions.**
- Level  $A_0$  contains the actions that could occur
  - **Conflicts between actions are represented by *mutex* links**

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## Cake example



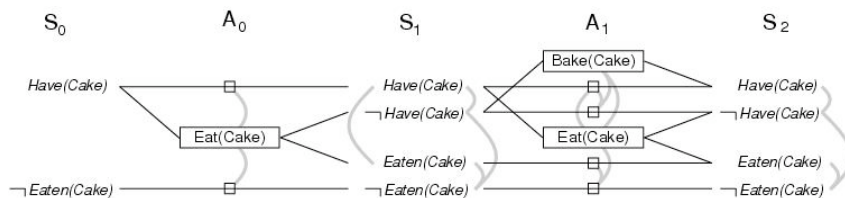
- Level  $S_1$  contains all literals that could result from picking any subset of actions in  $A_0$ 
  - **Conflicts between literals that can not occur together are represented by *mutex* links.**
  - **$S_1$  defines multiple states and the *mutex* links are the constraints that define this set of states.**
- Continue until two consecutive levels are identical: *leveled off*
  - **Or contain the same amount of literals (explanation follows later)**

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## Cake example



- A mutex relation holds between **two actions** when:
  - **Inconsistent effects:** one action negates the effect of another.
  - **Interference:** one of the effects of one action is the negation of a precondition of the other.
  - **Competing needs:** one of the preconditions of one action is mutually exclusive with the precondition of the other.
- A mutex relation holds between **two literals** when (*inconsistent support*):
  - **If one is the negation of the other OR**
  - **if each possible action pair that could achieve the literals is mutex.**

## PG and heuristic estimation

- PG's provide information about the problem
  - **A literal that does not appear in the final level of the graph cannot be achieved by any plan.**
    - Useful for backward search (cost = inf).
  - **Level of appearance can be used as cost estimate of achieving any goal literals = level cost.**
  - **Small problem: several actions can occur**
    - Restrict to one action using serial PG (add mutex links between every pair of actions, except persistence actions).
  - **Max-level, sum-level and set-level heuristics.**

PG is a relaxed problem.

# The GRAPHPLAN Algorithm

- How to extract a solution directly from the PG

```

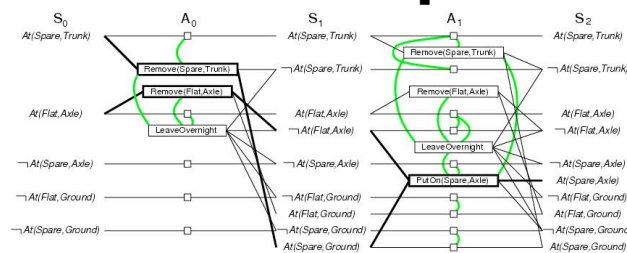
function GRAPHPLAN(problem) return solution or failure
  graph ← INITIAL-PLANNING-GRAPH(problem)
  goals ← GOALS[problem]
  loop do
    if goals all non-mutex in last level of graph then do
      solution ← EXTRACT-SOLUTION(graph, goals, LENGTH(graph))
      if solution ≠ failure then return solution
      else if NO-SOLUTION-POSSIBLE(graph) then return failure
    graph ← EXPAND-GRAPH(graph, problem)
  
```

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## GRAPHPLAN example



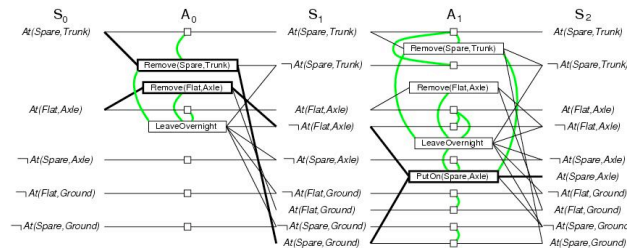
- Initially the plan consist of 5 literals from the initial state and the CWA literals (S0).
- Add actions whose preconditions are satisfied by EXPAND-GRAPH (A0)
- Also add persistence actions and mutex relations.
- Add the effects at level S1
- Repeat until goal is in level Si

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## GRAPHPLAN example



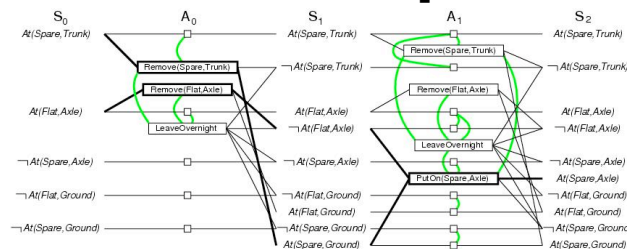
- EXPAND-GRAPH also looks for mutex relations
  - **Inconsistent effects**
    - E.g. Remove(Spare, Trunk) and LeaveOvernight
  - **Interference**
    - E.g. Remove(Flat, Axle) and LeaveOvernight
  - **Competing needs**
    - E.g. PutOn(Spare, Axle) and Remove(Flat, Axle)
  - **Inconsistent support**
    - E.g. in S2, At(Spare, Axle) and At(Flat, Axle)

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## GRAPHPLAN example



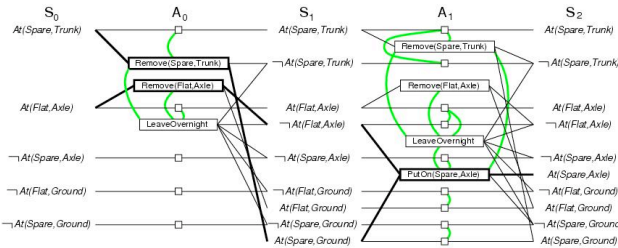
- In S2, the goal literal exists and is not mutex with any other
  - **Solution might exist and EXTRACT-SOLUTION will try to find it**
- EXTRACT-SOLUTION can use Boolean CSP to solve the problem or a search process:
  - **Initial state = last level of PG and goal goals of planning problem**
  - **Actions = select any set of non-conflicting actions that cover the goals in the state**
  - **Goal = reach level S0 such that all goals are satisfied**
  - **Cost = 1 for each action.**

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## GRAPHPLAN example



- Termination? YES
- PG are monotonically increasing or decreasing:
  - Literals increase monotonically
  - Actions increase monotonically
  - Mutexes decrease monotonically
- Because of these properties and because there is a finite number of actions and literals, every PG will eventually level off !

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## Planning with propositional logic

- Planning can be done by proving theorem in situation calculus.
- Here: test the *satisfiability* of a logical sentence:

$$\text{initial state} \wedge \text{all possible action descriptions} \wedge \text{goal}$$

- Sentence contains propositions for every action occurrence.
  - A model will assign true to the actions that are part of the correct plan and false to the others
  - An assignment that corresponds to an incorrect plan will not be a model because of inconsistency with the assertion that the goal is true.
  - If the planning is unsolvable the sentence will be unsatisfiable.

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TLo (IRIDIA)

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## SATPLAN algorithm

```
function SATPLAN(problem,  $T_{max}$ ) return solution or failure
  inputs: problem, a planning problem
          $T_{max}$ , an upper limit to the plan length
  for  $T = 0$  to  $T_{max}$  do
    cnf, mapping  $\leftarrow$  TRANSLATE-TO_SAT(problem,  $T$ )
    assignment  $\leftarrow$  SAT-SOLVER(cnf)
    if assignment is not null then
      return EXTRACT-SOLUTION(assignment, mapping)
  return failure
```

***cnf*, *mapping*  $\leftarrow$  TRANSLATE-TO\_SAT(*problem*,  $T$ )**

- Distinct propositions for assertions about each time step.
  - **Superscripts denote the time step**  
 $At(P1, SFO)^0 \wedge At(P2, JFK)^0$
  - **No CWA thus specify which propositions are not true**  
 $\neg At(P1, SFO)^0 \wedge \neg At(P2, JFK)^0$
  - **Unknown propositions are left unspecified.**
- The goal is associated with a particular time-step
  - **But which one?**

***cnf, mapping* ← TRANSLATE-TO\_SAT(*problem, T*)**

- How to determine the time step where the goal will be reached?
  - **Start at  $T=0$** 
    - Assert  $At(P1,SFO)^0 \wedge At(P2,JFK)^0$
  - **Failure .. Try  $T=1$** 
    - Assert  $At(P1,SFO)^1 \wedge At(P2,JFK)^1$
  - ...
  - **Repeat this until some minimal path length is reached.**
  - **Termination is ensured by  $T_{max}$**

***cnf, mapping* ← TRANSLATE-TO\_SAT(*problem, T*)**

- How to encode actions into PL?
  - **Propositional versions of successor-state axioms**  
 $At(P1,JFK)^t \Leftrightarrow$   
 $(At(P1,JFK)^0 \wedge \neg(Fly(P1,JFK,SFO)^0 \wedge At(P1,JFK)^0)) \vee$   
 $(Fly(P1,SFO,JFK)^0 \wedge At(P1,SFO)^0)$
  - **Such an axiom is required for each plane, airport and time step**
  - **If more airports add another way to travel than additional disjuncts are required**
- Once all these axioms are in place, the satisfiability algorithm can start to find a plan.

## **assignment** ← **SAT-SOLVER(cnf)**

- Multiple models can be found
- They are NOT satisfactory: (for  $T=1$ )  
 $Fly(P1,SFO,JFK)^0 \wedge Fly(P1,JFK,SFO)^0 \wedge Fly(P2,JFK,SFO)^0$   
The second action is infeasible  
Yet the plan IS a model of the sentence

*initial state*  $\wedge$  *all possible action descriptions*  $\wedge$  *goal*<sup>1</sup>

- Avoiding illegal actions: pre-condition axioms  
 $Fly(P1,SFO,JFK)^0 \Rightarrow At(P1,JFK)$
- Exactly one model now satisfies all the axioms where the goal is achieved at  $T=1$ .

## **assignment** ← **SAT-SOLVER(cnf)**

- A plane can fly at two destinations at once
- They are NOT satisfactory: (for  $T=1$ )  
 $Fly(P1,SFO,JFK)^0 \wedge Fly(P2,JFK,SFO)^0 \wedge Fly(P2,JFK,LAX)^0$   
The second action is infeasible  
Yet the plan allows spurious relations
- Avoid spurious solutions: action-exclusion axioms  
 $\neg(Fly(P2,JFK,SFO)^0 \wedge Fly(P2,JFK,LAX))$

**Prevents simultaneous actions**

- Lost of flexibility since plan becomes totally ordered : no actions are allowed to occur at the same time.
  - **Restrict exclusion to preconditions**



## Analysis of planning approach

- Planning is an area of great interest within AI
  - **Search for solution**
  - **Constructively prove a existence of solution**
- Biggest problem is the combinatorial explosion in states.
- Efficient methods are under research
  - **E.g. divide-and-conquer**