

Based on ppt slides for CMSC 421 by B.J. Dorr

Artificial Intelligence I: knowledge representation

Lecturer: Tom Lenaerts

Institut de Recherches Interdisciplinaires et de
Développements en Intelligence Artificielle
(IRIDIA). Université Libre de Bruxelles

Outline

- Ontological engineering
- Categories and objects
- Actions, situations and events
- Mental events and mental objects
- The internet shopping world
- Reasoning systems for categories
- Reasoning with default information
- Truth maintenance systems

Ontological engineering

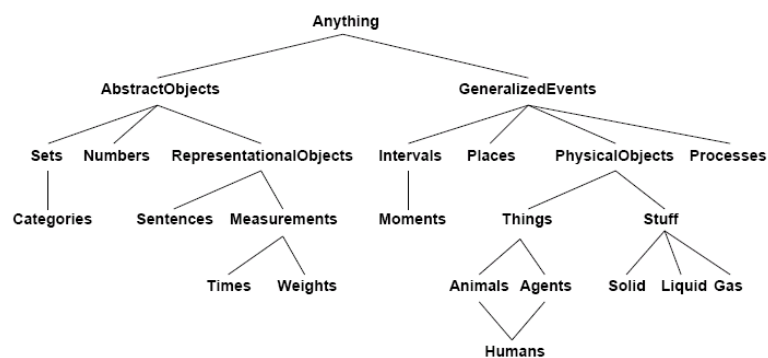
- How to create more general and flexible representations.
 - **Concepts like actions, time, physical object and beliefs**
 - **Operates on a bigger scale than K.E.**
- Define general framework of concepts
 - **Upper ontology**
- Limitations of logic representation
 - **Red, green and yellow tomatoes: exceptions and uncertainty**

December 6, 2004

TLo (IRIDIA)

3

The upper ontology of the world



December 6, 2004

TLo (IRIDIA)

4

Difference with special-purpose ontologies

- A general-purpose ontology should be applicable in more or less any special-purpose domain.
 - **Add domain-specific axioms**
- In any sufficiently demanding domain different areas of knowledge need to be unified.
 - **Reasoning and problem solving could involve several areas simultaneously**
- What do we need to express?
Categories, Measures, Composite objects, Time, Space, Change, Events, Processes, Physical Objects, Substances, Mental Objects, Beliefs

December 6, 2004

TLo (IRIDIA)

5

Categories and objects

- KR requires the organisation of objects into categories
 - **Interaction at the level of the object**
 - **Reasoning at the level of categories**
- Categories play a role in predictions about objects
 - **Based on perceived properties**
- Categories can be represented in two by FOL
 - **Predicates: apple(x)**
 - **Reification of categories into objects: apples**
- Category = set of its members

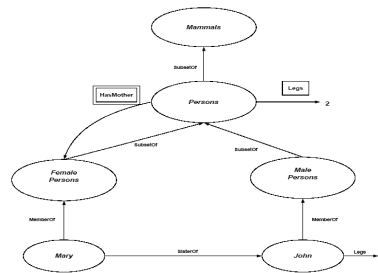
December 6, 2004

TLo (IRIDIA)

6

Category organization

- Relation = *inheritance*:
 - All instance of food are edible, fruit is a subclass of food and apples is a subclass of fruit then an applied is edible.
- Defines a taxonomy



December 6, 2004

TLo (IRIDIA)

7

FOL and categories

- An object is a member of a category
 - **MemberOf(BB₁₂, Basketballs)**
- A category is a subclass of another category
 - **SubsetOf(Basketballs, Balls)**
- All members of a category has some properties
 - $\forall x (\text{MemberOf}(x, \text{Basketballs}) \Rightarrow \text{Round}(x))$
- All members of a category can be recognized by some properties
 - $\forall x (\text{Orange}(x) \wedge \text{Round}(x) \wedge \text{Diameter}(x)=9.5\text{in} \wedge \text{MemberOf}(x, \text{Balls}) \Rightarrow \text{MemberOf}(x, \text{BasketBalls}))$
- A category as a whole has some properties
 - **MemberOf(Dogs, DomesticatedSpecies)**

December 6, 2004

TLo (IRIDIA)

8

Relations between categories

- Two or more categories are *disjoint* if they have no members in common:
 - **Disjoint(s)** $\Leftrightarrow (\forall c_1, c_2 \ c_1 \in s \wedge c_2 \in s \wedge c_1 \neq c_2 \Rightarrow \text{Intersection}(c_1, c_2) = \{\})$
 - **Example; Disjoint({animals, vegetables})**
- A set of categories s constitutes an *exhaustive decomposition* of a category c if all members of the set c are covered by categories in s :
 - **E.D.(s,c)** $\Leftrightarrow (\forall i \ i \in c \Rightarrow \exists c_2 \ c_2 \in s \wedge i \in c_2)$
 - **Example: ExhaustiveDecomposition({Americans, Canadian, Mexicans}, NorthAmericans).**

Relations between categories

- A *partition* is a disjoint exhaustive decomposition:
 - **Partition(s,c)** $\Leftrightarrow \text{Disjoint}(s) \wedge \text{E.D.}(s,c)$
 - **Example: Partition({Males, Females}, Persons).**
- Is ({Americans, Canadian, Mexicans}, NorthAmericans) a partition?
- Categories can be defined by providing necessary and sufficient conditions for membership
 - ◆ $\forall x \ \text{Bachelor}(x) \Leftrightarrow \text{Male}(x) \wedge \text{Adult}(x) \wedge \text{Unmarried}(x)$

Natural kinds

- Many categories have no clear-cut definitions (chair, bush, book).
- Tomatoes: sometimes green, red, yellow, black. Mostly round.
- One solution: category *Typical(Tomatoes)*.
 - $\forall x, x \in \text{Typical(Tomatoes)} \Rightarrow \text{Red}(x) \wedge \text{Spherical}(x)$.
 - **We can write down useful facts about categories without providing exact definitions.**
- What about “bachelor”? Quine challenged the utility of the notion of *strict definition*. We might question a statement such as “the Pope is a bachelor”.

December 6, 2004

TLo (IRIDIA)

11

Physical composition

- One object may be part of another:
 - **PartOf(Bucharest,Romania)**
 - **PartOf(Romania,EasternEurope)**
 - **PartOf(EasternEurope,Europe)**
- The PartOf predicate is transitive (and irreflexive), so we can infer that PartOf(Bucharest,Europe)
- More generally:
 - $\forall x \text{ PartOf}(x,x)$
 - $\forall x,y,z \text{ PartOf}(x,y) \wedge \text{PartOf}(y,z) \Rightarrow \text{PartOf}(x,z)$
- Often characterized by structural relations among parts.
 - **E.g. Biped(a) \Rightarrow**
$$(\exists l_1, l_2, b)(\text{Leg}(l_1) \wedge \text{Leg}(l_2) \wedge \text{Body}(b) \wedge$$
$$\text{PartOf}(l_1, a) \wedge \text{PartOf}(l_2, a) \wedge \text{PartOf}(b, a) \wedge$$
$$\text{Attached}(l_1, b) \wedge \text{Attached}(l_2, b) \wedge$$
$$l_1 \neq l_2 \wedge (\forall l_3)(\text{Leg}(l_3) \Rightarrow (l_3 = l_1 \vee l_3 = l_2)))$$

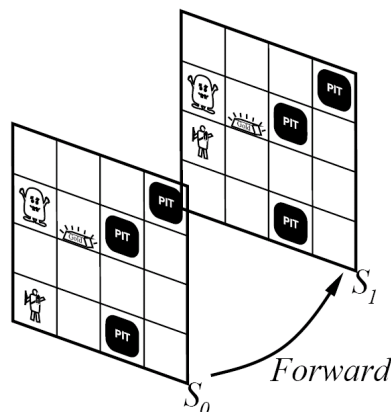
December 6, 2004

12

Measurements

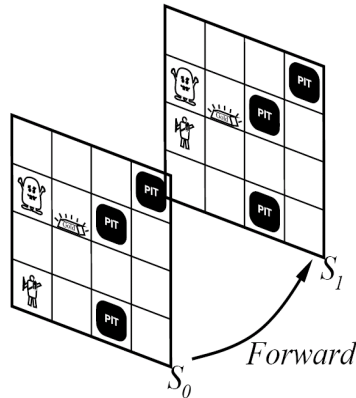
- Objects have height, mass, cost,
Values that we assign to these are **measures**
- Combine Unit functions with a number: $\text{Length}(L_1) = \text{Inches}(1.5) = \text{Centimeters}(3.81)$.
- Conversion between units:
 $\forall i \text{ Centimeters}(2.54 \times i) = \text{Inches}(i)$.
- Some measures have no scale: Beauty, Difficulty, etc.
 - **Most important aspect of measures: is that they are orderable.**
 - **Don't care about the actual numbers. (An apple can have deliciousness .9 or .1.)**

Actions, events and situations



- Reasoning about outcome of actions is central to KB-agent.
- How can we keep track of location in FOL?
 - **Remember the multiple copies in PL.**
- Representing time by situations (states resulting from the execution of actions).
 - **Situation calculus**

Actions, events and situations



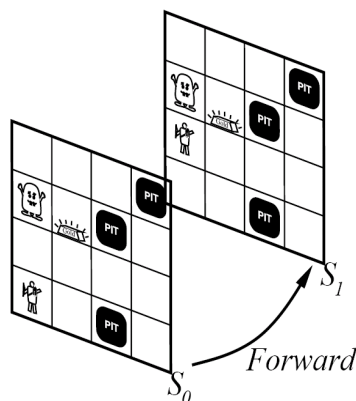
- Situation calculus:
 - **Actions are logical terms**
 - **Situations are logical terms consisting of**
 - The initial situation I
 - All situations resulting from the action on I ($=Result(a,s)$)
 - **Fluent are functions and predicates that vary from one situation to the next.**
 - E.g. $\neg Holding(G_1, S_0)$
 - **Eternal predicates are also allowed**
 - E.g. $Gold(G_1)$

December 6, 2004

TLo (IRIDIA)

15

Actions, events and situations



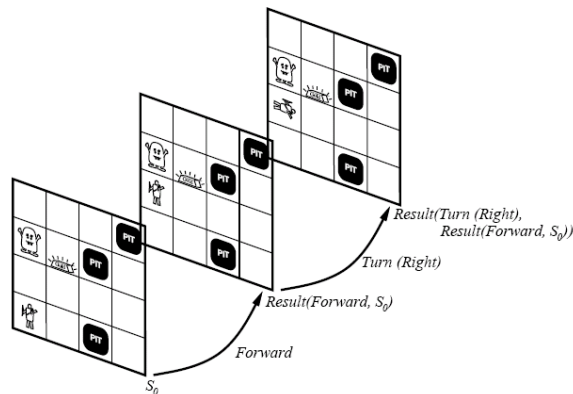
- Results of action sequences are determined by the individual actions.
- *Projection task*: an SC agent should be able to deduce the outcome of a sequence of actions.
- *Planning task*: find a sequence that achieves a desirable effect

December 6, 2004

TLo (IRIDIA)

16

Actions, events and situations



December 6, 2004

TLo (IRIDIA)

17

Describing change

- Simple Situation calculus requires to axioms to describe change:

- **Possibility axiom: when is it possible to do the action**

$$At(Agent, x, s) \wedge Adjacent(x, y) \Rightarrow Poss(Go(x, y), s)$$

- **Effect axiom: describe changes due to action**

$$Poss(Go(x, y), s) \Rightarrow At(Agent, y, Result(Go(x, y), s))$$

- What stays the same?

- **Frame problem: how to represent all things that stay the same?**

- **Frame axiom: describe non-changes due to actions**

$$At(o, x, s) \wedge (o \neq Agent) \wedge \neg Holding(o, s) \Rightarrow At(o, x, Result(Go(y, z), s))$$

December 6, 2004

TLo (IRIDIA)

18

Representational frame problem

- If there are F fluents and A actions then we need AF frame axioms to describe other objects are stationary unless they are held.
 - **We write down the effect of each actions**
- Solution; describe how each fluent changes over time
 - **Successor-state axiom:**
$$Pos(a,s) \Rightarrow (At(Agent,y,Result(a,s)) \Leftrightarrow (a = Go(x,y)) \vee (At(Agent,y,s) \wedge a \neq Go(y,z)))$$
 - **Note that next state is completely specified by current state.**
 - **Each action effect is mentioned only once.**

Other problems

- How to deal with secondary (implicit) effects?
 - **If the agent is carrying the gold and the agent moves then the gold moves too.**
 - **Ramification problem**
- How to decide whether fluents hold in the future?
 - **Inferential frame problem.**

Mental events and objects

- So far, KB agents can have beliefs and deduce new beliefs
- What about knowledge about beliefs? What about knowledge about the inference proces?
 - **Requires a model of the mental objects in someone's head and the processes that manipulate these objects.**
- Relationships between agents and mental objects: believes, knows, wants, ...
 - **Believes(Lois,Flies(Superman)) with Flies(Superman) being a function ... a candidate for a mental object (reification).**
 - **Agent can now reason about the beliefs of agents.**

December 6, 2004

TLo (IRIDIA)

21

The internet shopping world

- A Knowledge Engineering example
- An agent that helps a buyer to find product offers on the internet.
 - **IN = product description (precise or -precise)**
 - **OUT = list of webpages that offer the product for sale.**
- Environment = WWW
- Percepts = web pages (character strings)
 - **Extracting useful information required.**

December 6, 2004

TLo (IRIDIA)

22

The internet shopping world

- Find relevant product offers
 - $RelevantOffer(page, url, query) \Leftrightarrow Relevant(page, url, query) \wedge Offer(page)$
 - **Write axioms to define Offer(x)**
 - **Find relevant pages: Relevant(x,y,z) ?**
 - Start from an initial set of stores.
 - What is a relevant category?
 - What are relevant connected pages?
 - **Require rich category vocabulary.**
 - Synonymy and ambiguity
 - **How to retrieve pages: GetPage(url)?**
 - Procedural attachment
- Compare offers (information extraction).

Reasoning systems for categories

- How to organise and reason with categories?
 - **Semantic networks**
 - Visualize knowledge-base
 - Efficient algorithms for category membership inference
 - **Description logics**
 - Formal language for constructing and combining category definitions
 - Efficient algorithms to decide subset and superset relationships between categories.

Semantic Networks

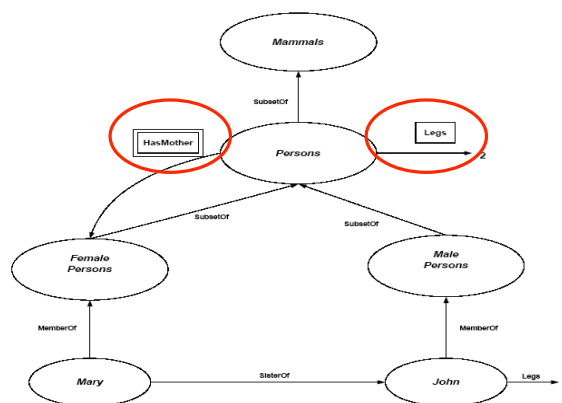
- Logic vs. semantic networks
- Many variations
 - **All represent individual objects, categories of objects and relationships among objects.**
- Allows for inheritance reasoning
 - **Female persons inherit all properties from person.**
 - **Cfr. OO programming.**
- Inference of inverse links
 - **SisterOf vs. HasSister**

December 6, 2004

TLo (IRIDIA)

25

Semantic network example



December 6, 2004

TLo (IRIDIA)

26

Semantic networks

- Drawbacks
 - **Links can only assert binary relations**
 - **Can be resolved by reification of the proposition as an event**
- Representation of default values
 - **Enforced by the inheritance mechanism.**

December 6, 2004

TLo (IRIDIA)

27

Description logics

- Are designed to describe definitions and properties about categories
 - **A formalization of semantic networks**
- Principal inference task is
 - **Subsumption: checking if one category is the subset of another by comparing their definitions**
 - **Classification: checking whether an object belongs to a category.**
 - **Consistency: whether the category membership criteria are logically satisfiable.**

December 6, 2004

TLo (IRIDIA)

28

Reasoning with Default Information

- “The following courses are offered: CS101, CS102, CS106, EE101”
 - Four (db)
 - **Assume that this information is complete (not asserted ground atomic sentences are false)**
= CLOSED WORLD ASSUMPTION
 - **Assume that distinct names refer to distinct objects**
= UNIQUE NAMES ASSUMPTION
 - Between one and infinity (logic)
 - **Does not make these assumptions**
 - **Requires completion.**

Truth maintenance systems

- Many of the inferences have default status rather than being absolutely certain
 - **Inferred facts can be wrong and need to be retracted = BELIEF REVISION.**
 - **Assume KB contains sentence P and we want to execute TELL(KB, -P)**
 - To avoid contradiction: RETRACT(KB,P)
 - But what about sentences inferred from P?
- Truth maintenance systems are designed to handle these complications.